# **Supercomputing in Plain English** Shared Memory Multithreading

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### Outline

Parallelism

### Shared Memory Parallelism

OpenMP



# Parallelism

### Parallelism

**Parallelism** means doing multiple things at the same time: you can get more work done in the same amount of time.

































More fish!



## What Is Parallelism?

**<u>Parallelism</u>** is the use of multiple processing units – either processors or parts of an individual processor – to solve a problem, and in particular the use of multiple processing units operating concurrently on different parts of a problem.

The different parts could be different tasks, or the same task on different pieces of the problem's data.



## **Kinds of Parallelism**

- Shared Memory Multithreading (our topic today)
- Distributed Memory Multiprocessing (next time)
- Hybrid Shared/Distributed



## Why Parallelism Is Good

- <u>The Trees</u>: We like parallelism because, as the number of processing units working on a problem grows, we can solve <u>the same problem in less</u> <u>time</u>.
- <u>The Forest</u>: We like parallelism because, as the number of processing units working on a problem grows, we can solve <u>bigger problems</u>.



# **Parallelism Jargon**

- <u>Threads</u>: execution sequences that share a single memory area ("<u>address space</u>")
- <u>Processes</u>: execution sequences with their own independent, private memory areas
- ... and thus:
- <u>*Multithreading*</u>: parallelism via multiple threads
- *Multiprocessing*: parallelism via multiple processes

As a general rule, Shared Memory Parallelism is concerned with <u>threads</u>, and Distributed Parallelism is concerned with <u>processes</u>.



# **Jargon Alert**

In principle:

- "shared memory parallelism" → "multithreading"
- "distributed parallelism" → "multiprocessing"

In practice, these terms are often used interchangeably:

- Parallelism
- *Concurrency* (not as popular these days)
- Multithreading
- Multiprocessing
- Typically, you have to figure out what is meant based on the context.



### **Amdahl's Law**

In 1967, Gene Amdahl came up with an idea so crucial to our understanding of parallelism that they named a Law for him:

$$S = \frac{1}{(1 - F_p) + \frac{F_p}{S_p}}$$

where *S* is the overall speedup achieved by parallelizing a code,  $F_p$  is the fraction of the code that's parallelizable, and  $S_p$  is the speedup achieved in the parallel part.<sup>[1]</sup>



# **Amdahl's Law: Huh?**

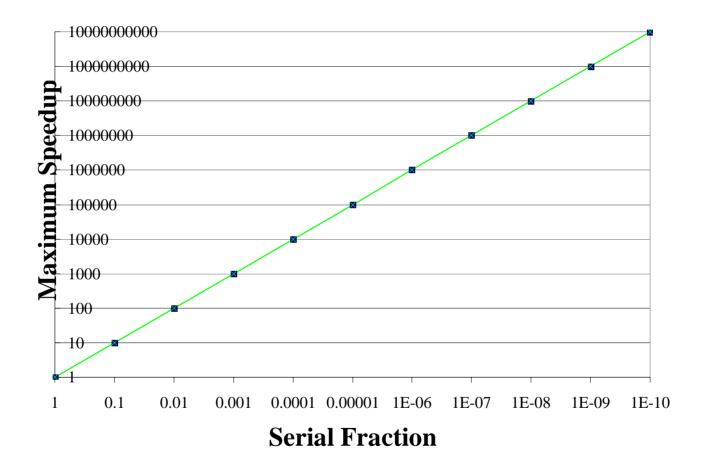
What does Amdahl's Law tell us? Well, imagine that you run your code on a zillion processors. The parallel part of the code could exhibit up to a factor of a zillion speedup. For sufficiently large values of a zillion, the **parallel part would take** <u>zero time</u>!

But, the <u>serial</u> (non-parallel) part would take the <u>same amount of time as on a single processor</u>.

So running your code on infinitely many processors would still take at least as much time as it takes to run just the serial part.



# Max Speedup by Serial %





### **Amdahl's Law Example**

```
PROGRAM amdahl_test
IMPLICIT NONE
REAL,DIMENSION(a_lot) :: array
REAL :: scalar
INTEGER :: index
READ *, scalar !! Serial part
DO index = 1, a_lot !! Parallel part
array(index) = scalar * index
END DO !! index = 1, a_lot
END PROGRAM amdahl_test
```

If we run this program on infinitely many CPUs, then the total run time will still be at least as much as the time it takes to perform the **READ**.



### The Point of Amdahl's Law

**<u>Rule of Thumb</u>**: When you write a parallel code, try to make as much of the code parallel as possible, because the **serial part will be the limiting factor** on parallel speedup.

Note that this rule will not hold when the *overhead* cost of parallelizing exceeds the parallel speedup. More on this presently.



# Speedup

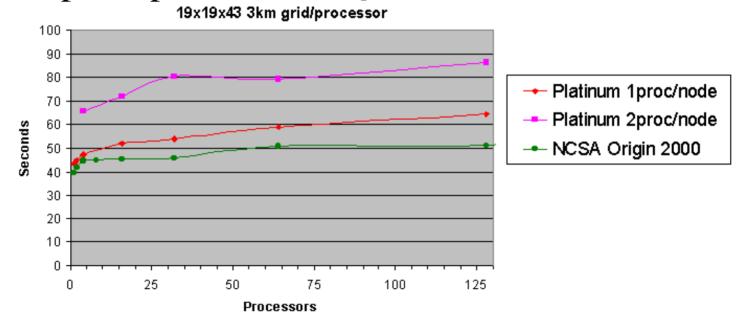
The goal in parallelism is *linear speedup*: getting the speed of the job to increase by a factor equal to the number of processors.

Very few programs actually exhibit linear speedup, but some come close.



### **Scalability**

### <u>Scalable</u> means "performs just as well regardless of how big the problem is." A scalable code has near linear speedup. ARPS Benchmark Timings



Platinum = NCSA 1024 processor PIII/1GHZ Linux Cluster Note: NCSA Origin timings are scaled from 19x19x53 domains.



# Granularity

<u>Granularity</u> is the size of the subproblem that each thread or process works on, and in particular the size that it works on between communicating or synchronizing with the others.

- Some codes are *coarse grain* (a few very big parallel parts) and some are *fine grain* (many little parallel parts).
- Usually, coarse grain codes are more scalable than fine grain codes, because less time is spent managing the parallelism, so more is spent getting the work done.



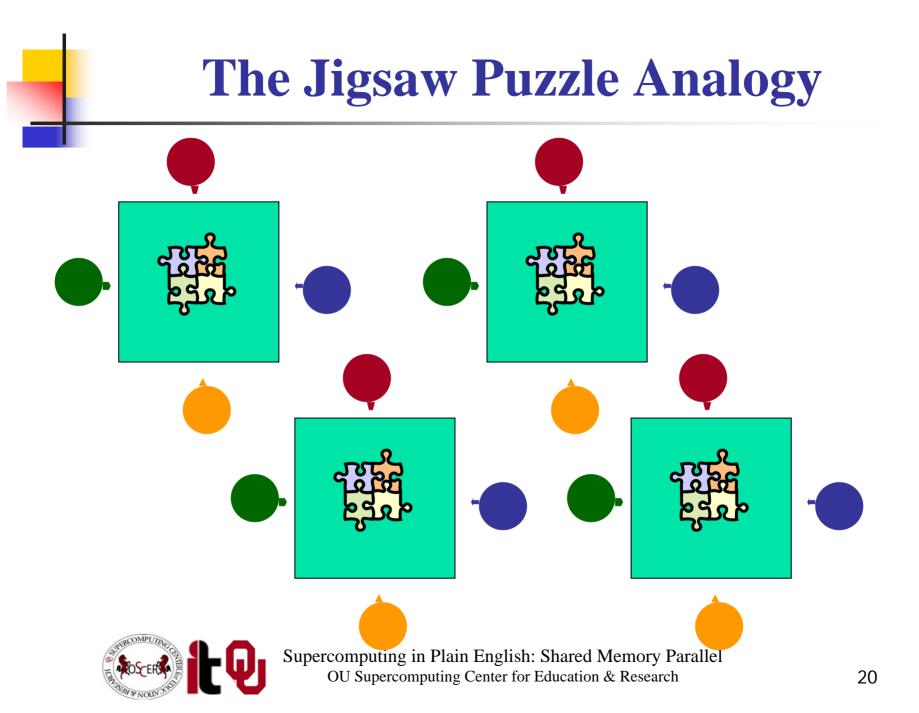
## **Parallel Overhead**

Parallelism isn't free. Behind the scenes, the compiler and the hardware have to do a lot of overhead work to make parallelism happen.
The overhead typically includes:

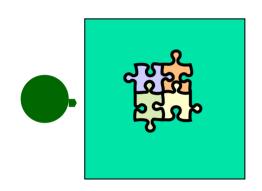
- Managing the multiple threads/processes
- <u>Communication</u> among threads/processes
- Synchronization (described later)



# Shared Memory Parallelism



# **Serial Computing**

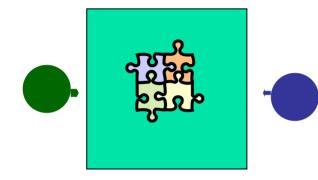


Suppose you want to do a jigsaw puzzle that has, say, a thousand pieces.

We can imagine that it'll take you a certain amount of time. Let's say that you can put the puzzle together in an hour.



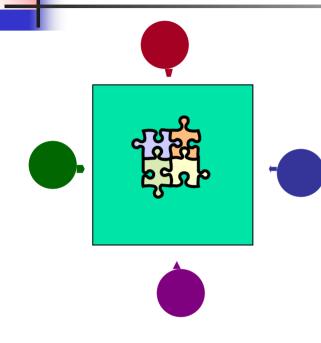
### **Shared Memory Parallelism**



If Julie sits across the table from you, then she can work on her half of the puzzle and you can work on yours. Once in a while, you'll both reach into the pile of pieces at the same time (you'll *contend* for the same resource), which will cause a little bit of slowdown. And from time to time you'll have to work together (*communicate*) at the interface between her half and yours. The speedup will be nearly 2-to-1: y'all might take 35 minutes instead of 30.



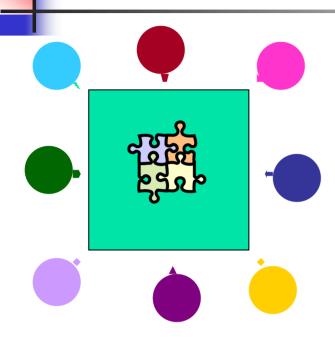
# **The More the Merrier?**



Now let's put Lloyd and Jerry on the other two sides of the table. Each of you can work on a part of the puzzle, but there'll be a lot more contention for the shared resource (the pile of puzzle pieces) and a lot more communication at the interfaces. So y'all will get noticeably less than a 4-to-1 speedup, but you'll still have an improvement, maybe something like 3-to-1: the four of you can get it done in 20 minutes instead of an hour.



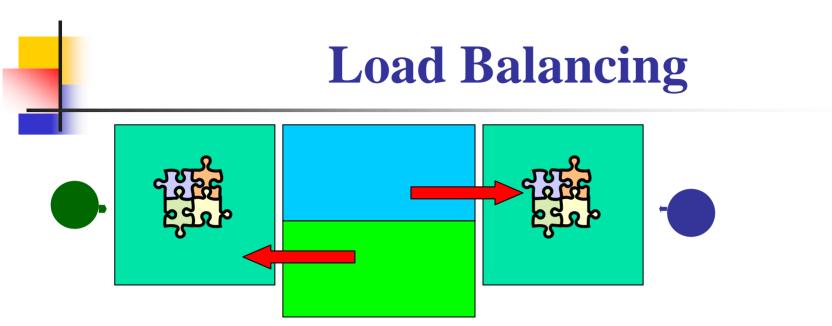
# **Diminishing Returns**



If we now put Dave and Paul and Tom and Charlie on the corners of the table, there's going to be a whole lot of contention for the shared resource, and a lot of communication at the many interfaces. So the speedup y'all get will be much less than we'd like; you'll be lucky to get 5-to-1.

So we can see that adding more and more workers onto a shared resource is eventually going to have a diminishing return.



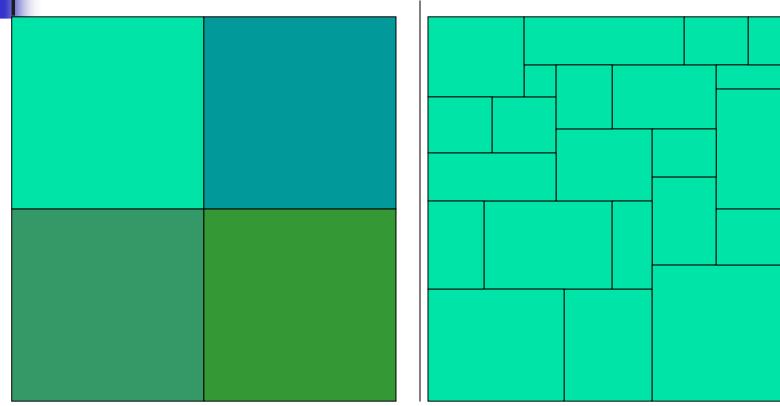


*Load balancing* means giving everyone roughly the same amount of work to do.

For example, if the jigsaw puzzle is half grass and half sky, then you can do the grass and Julie can do the sky, and then y'all only have to communicate at the horizon – and the amount of work that each of you does on your own is roughly equal. So you'll get pretty good speedup.



# Load Balancing



Load balancing can be easy, if the problem splits up into chunks of roughly equal size, with one chunk per processor. Or load balancing can be very hard.



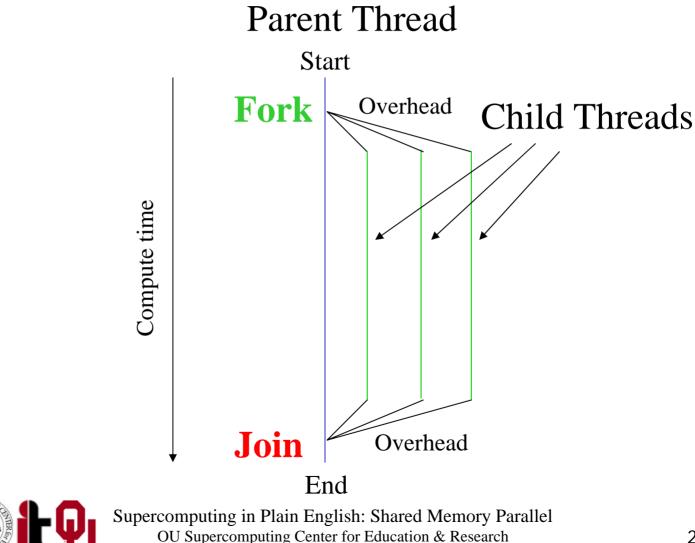
# **The Fork/Join Model**

Many shared memory parallel systems use a programming model called *Fork/Join*. Each program begins executing on just a single thread, called the *parent*.

- *Fork*: When a parallel region is reached, the master thread *spawns* additional *child* threads as needed.
- **Join**: When the parallel region ends, the child threads shut down, leaving only the parent still running.



## The Fork/Join Model (cont'd)



# The Fork/Join Model (cont'd)

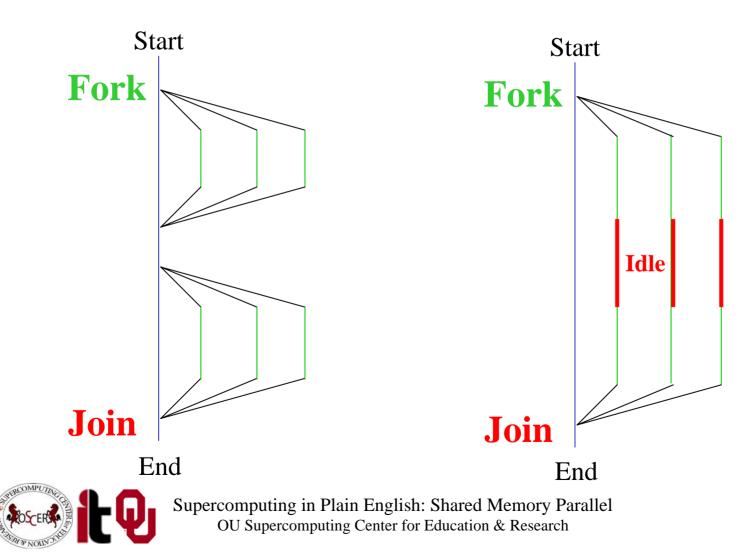
In principle, as a parallel section completes, the child threads shut down (join the parent), forking off again when the parent reaches another parallel section.

In practice, the child threads often continue to exist but are <u>idle</u>.

Why?



### **Principle vs. Practice**



# Why Idle?

- On some shared memory multithreading computers, the overhead cost of forking and joining is high compared to the cost of computing, so rather than waste time on overhead, the children simply sit idle until the next parallel section.
- On some computers, joining threads releases a program's control over the child processors, so they may not be available for more parallel work later in the run. *Gang scheduling* is preferable, because then all of the processors are guaranteed to be available for the whole run.





Most of this discussion is from [2], with a little bit from [3].

# What Is OpenMP?

OpenMP is a standardized way of expressing shared memory parallelism.

# OpenMP consists of *compiler directives*, *functions* and *environment variables*.

- When you compile a program that has OpenMP in it, if your compiler knows OpenMP, then you get an executable that can run in parallel; otherwise, the compiler ignores the OpenMP stuff and you get a purely serial executable.
- OpenMP can be used in Fortran, C and C++, but only if your preferred compiler explicitly supports it.



# **Compiler Directives**

- A <u>compiler directive</u> is a line of source code that gives the compiler special information about the statement or block of code that immediately follows.
- C++ and C programmers already know about compiler directives:

### #include "MyClass.h"

Many Fortran programmers already have seen at least one compiler directive:

#### INCLUDE 'mycommon.inc'



# **OpenMP Compiler Directives**

OpenMP compiler directives in Fortran look like this: **!\$OMP** ....**stuff**...

In C++ and C, OpenMP directives look like: **#pragma omp**...*stuff*...

- Both directive forms mean "the rest of this line contains OpenMP information."
- Aside: "*pragma*" is the Greek word for "thing." Go figure.



## **Example OpenMP Directives**

Fortran

- **!\$OMP PARALLEL DO**
- **!\$OMP CRITICAL**
- **!\$OMP MASTER**
- **!\$OMP BARRIER**
- **!\$OMP SINGLE**
- **!\$OMP ATOMIC**
- **!\$OMP SECTION**
- **!\$OMP FLUSH**
- **!\$OMP ORDERED**

C++/C

#pragma omp parallel for #pragma omp critical #pragma omp master #pragma omp barrier #pragma omp single #pragma omp atomic #pragma omp section #pragma omp flush #pragma omp ordered

### Note that we won't cover all of these.



#### A First OpenMP Program

```
PROGRAM hello world
  IMPLICIT NONE
  INTEGER :: number of threads, this thread, iteration
  number of threads = omp get max threads()
  WRITE (0,"(I2,A)") number of threads, " threads"
!SOMP PARALLEL DO DEFAULT(PRIVATE) &
! SOMP
                  SHARED(number of threads)
  DO iteration = 0, number of threads - 1
    this thread = omp get thread num()
    WRITE (0,"(A,I2,A,I2,A) ")"Iteration ", &
      iteration, ", thread ", this thread, &
 Se .
      ": Hello, world!"
 <u>ک</u>
  END DO
END PROGRAM hello world
```



#### Running hello\_world

<pre>% setenv OMP_NUM_THREADS 4</pre>					
% hello_world					
4 threads					
Iteration	0,	thread	0:	Hello,	world!
Iteration	1,	thread	1:	Hello,	world!
Iteration	З,	thread	3:	Hello,	world!
Iteration	2,	thread	2:	Hello,	world!
% hello_world					
4 threads					
Iteration	2,	thread	2:	Hello,	world!
Iteration	1,	thread	1:	Hello,	world!
Iteration	0,	thread	0:	Hello,	world!
Iteration	3,	thread	3:	Hello,	world!
% hello_world					
4 threads					
Iteration	1,	thread	1:	Hello,	world!
Iteration	2,	thread	2:	Hello,	world!
Iteration	0,	thread	0:	Hello,	world!
Iteration	3,	thread	3:	Hello,	world!



#### **OpenMP Issues Observed**

From the **hello\_world** program, we learn that:

 at some point before running an OpenMP program, you must set an environment variable

**OMP\_NUM\_THREADS** 

that represents the number of threads to use;

 the order in which the threads execute is nondeterministic.



The **PARALLEL DO** directive tells the compiler that the **DO** loop immediately after the directive should be executed in parallel; for example:

```
!$OMP PARALLEL DO
```

```
DO index = 1, length
    array(index) = index * index
END DO
```

The iterations of the loop will be computed in parallel (note that they are independent of one another).



#### A Change to hello\_world

Suppose we do 3 loop iterations per thread: DO iteration = 0, number\_of\_threads \* 3 - 1

- % hello\_world
- 4 threads

Iteration 9, thread 3: Hello, world! Iteration 0, thread 0: Hello, world! Iteration 10, thread 3: Hello, world! Iteration 11, thread 3: Hello, world! Iteration 1, thread 0: Hello, world! 0: Hello, world! Iteration 2, thread Iteration 3, thread 1: Hello, world! Iteration 6, thread 2: Hello, world! 2: Hello, world! Iteration 7, thread Iteration 8, thread 2: Hello, world! Iteration 4. thread 1: Hello, world! Iteration 5, thread 1: Hello, world!

Notice that the iterations are split into contiguous <u>chunks</u>, and each thread gets one chunk of iterations.



#### Chunks

- By default, OpenMP splits the iterations of a loop into chunks of equal (or roughly equal) size, assigns each chunk to a thread, and lets each thread loop through its subset of the iterations.
- So, for example, if you have 4 threads and 12 iterations, then each thread gets three iterations:
- Thread 0: iterations 0, 1, 2
- Thread 1: iterations 3, 4, 5
- Thread 2: iterations 6, 7, 8
- Thread 3: iterations 9, 10, 11

# Notice that each thread performs its own chunk in deterministic order, but that the overall order is nondeterministic.



#### **Private and Shared Data**

<u>*Private*</u> data are data that are owned by, and only visible to, a single individual thread.

<u>Shared</u> data are data that are owned by and visible to all threads.

(Note: in distributed computing, all data are private, as we'll see next time.)



#### **Should All Data Be Shared?**

In our example program, we saw this:

!\$OMP PARALLEL DO DEFAULT(PRIVATE) SHARED(number\_of\_threads)

What do **DEFAULT ( PRIVATE )** and **SHARED** mean?

- We said that OpenMP uses shared memory parallelism. So **PRIVATE** and **SHARED** refer to memory.
- Would it make sense for all data within a parallel loop to be shared?



#### A Private Variable

```
Consider this loop:
!$OMP PARALLEL DO ...
DO iteration = 0, number_of_threads - 1
this_thread = omp_get_thread_num()
WRITE (0,"(A,I2,A,I2,A) ") "Iteration ", iteration, &
& ", thread ", this_thread, ": Hello, world!"
END DO
```

- Notice that, if the iterations of the loop are executed concurrently, then the loop index variable named **iteration** will be wrong for all but one of the threads.
- Each thread should get its own copy of the variable named **iteration**.



#### **Another Private Variable**

```
!$OMP PARALLEL DO ...
DO iteration = 0, number_of_threads - 1
this_thread = omp_get_thread_num()
WRITE (0,"(A,I2,A,I2,A)") "Iteration ", iteration, &
& ", thread ", this_thread, ": Hello, world!"
END DO
```

- Notice that, if the iterations of the loop are executed concurrently, then **this\_thread** will be wrong for all but one of the threads.
- Each thread should get its own copy of the variable named **this\_thread**.



#### **A Shared Variable**

```
!$OMP PARALLEL DO ...
DO iteration = 0, number_of_threads - 1
this_thread = omp_get_thread_num()
WRITE (0,"(A,I2,A,I2,A)"") "Iteration ", iteration, &
& ", thread ", this_thread, ": Hello, world!"
END DO
```

```
Notice that, regardless of whether the iterations of the loop are executed serially or in parallel, number_of_threads will be correct for all of the threads.
```

All threads should share a single instance of **number\_of\_threads**.



#### SHARED & PRIVATE Clauses

The **PARALLEL DO** directive allows extra <u>clauses</u> to be appended that tell the compiler which variables are shared and which are private: !\$OMP PARALLEL DO PRIVATE(iteration,this\_thread) & !\$OMP SHARED (number\_of\_threads)
This tells that compiler that iteration and this\_thread are private but that number\_of\_threads is shared.

(Note the syntax for continuing a directive.)



#### **DEFAULT** Clause

If your loop has lots of variables, it may be cumbersome to put all of them into **SHARED** and **PRIVATE** clauses.

So, OpenMP allows you to declare one kind of data to be the default, and then you only need to explicitly declare variables of the other kind: !\$OMP PARALLEL DO DEFAULT(PRIVATE) & !\$OMP SHARED(number\_of\_threads)
The default DEFAULT (so to speak) is

**SHARED**, except for the loop index variable, which by default is **PRIVATE**.



#### **Different Workloads**

What happens if the threads have different amounts of work to do?

**!\$OMP PARALLEL DO** 

```
D0 index = 1, length
x(index) = index / 3.0
IF ((index / 1000) < 1) THEN
y(index) = LOG(x(index))
ELSE
y(index) = x(index) + 2
END IF
END DO</pre>
```

The threads that finish early have to wait.



#### Chunks

- By default, OpenMP splits the iterations of a loop into chunks of equal (or roughly equal) size, assigns each chunk to a thread, and lets each thread loop through its subset of the iterations.
- So, for example, if you have 4 threads and 12 iterations, then each thread gets three iterations:
- Thread 0: iterations 0, 1, 2
- Thread 1: iterations 3, 4, 5
- Thread 2: iterations 6, 7, 8
- Thread 3: iterations 9, 10, 11
- Notice that each thread performs its own chunk in deterministic order, but that the overall order is nondeterministic.



### **Scheduling Strategies**

OpenMP supports three scheduling strategies:

- <u>Static</u>: the default, as described in the previous slides good for iterations that are inherently load balanced
- Dynamic: each thread gets a chunk of a few iterations, and when it finishes that chunk it goes back for more, and so on until all of the iterations are done good when iterations aren't load balanced at all
- <u>*Guided*</u>: each thread gets smaller and smaller chunks over time a compromise



## **Static Scheduling**

For  $N_i$  iterations and  $N_t$  threads, each thread gets one chunk of  $N_i/N_t$  loop iterations:

- Thread #0: iterations 0 through  $N_i/N_t-1$
- Thread #1: iterations  $N_i/N_t$  through  $2N_i/N_t-1$
- Thread #2: iterations  $2N_i/N_t$  through  $3N_i/N_t-1$
- Thread  $\#N_t-1$ : iterations  $(N_t-1)N_i/N_t$  through  $N_i-1$



## **Dynamic Scheduling**

For  $N_i$  iterations and  $N_t$  threads, each thread gets a fixed-size chunk of *k* loop iterations:

- When a particular thread finishes its chunk of iterations, it gets assigned a new chunk. So, the relationship between iterations and threads is nondeterministic.
- Advantage: very flexible
- Disadvantage: high overhead lots of decision making about which thread gets each chunk



### **Guided Scheduling**

For  $N_i$  iterations and  $N_t$  threads, initially each thread gets a fixed-size chunk of  $k < N_i/N_t$  loop iterations:

- After each thread finishes its chunk of k iterations, it gets a chunk of k/2 iterations, then k/4, etc. Chunks are assigned dynamically, as threads finish their previous chunks.
- Advantage over static: can handle imbalanced load
- Advantage over dynamic: fewer decisions, so less overhead



#### **How to Know Which Schedule?**

Test all three using a typical case as a <u>benchmark</u>.
Whichever wins is probably the one you want to use most of the time on that particular platform.
This may vary depending on problem size, new versions of the compiler, who's on the machine, what day of the week it is, etc, so you may want to

benchmark the three schedules from time to time.



#### **SCHEDULE Clause**

The **PARALLEL DO** directive allows a **SCHEDULE** clause to be appended that tell the compiler which variables are shared and which are private:

!\$OMP PARALLEL DO ... SCHEDULE(STATIC)

- This tells that compiler that the schedule will be static.
- Likewise, the schedule could be **GUIDED** or **DYNAMIC**.
- However, the very best schedule to put in the **SCHEDULE** clause is **RUNTIME**.
- You can then set the environment variable **OMP\_SCHEDULE** to **STATIC** or **GUIDED** or **DYNAMIC** at runtime – great for benchmarking!



#### **Synchronization**

<u>Jargon</u>: waiting for other threads to finish a parallel loop (or other parallel section) before going on to the work after the parallel section is called <u>synchronization</u>.

Synchronization is bad, because when a thread is waiting for the others to finish, it isn't getting any work done, so it isn't contributing to speedup.

So why would anyone ever synchronize?



#### Why Synchronize?

Synchronizing is necessary when the code that follows a parallel section needs all threads to have their final answers.

```
!$OMP PARALLEL DO
DO index = 1, length
    x(index) = index / 1024.0
    IF ((index / 1000) < 1) THEN
        y(index) = LOG(x(index))
    ELSE
        y(index) = x(index) + 2
    END IF
END DO
! Need to synchronize here!
DO index = 1, length
    z(index) = y(index) + y(length - index + 1)
END DO
```



#### Barriers

- A *barrier* is a place where synchronization is forced to occur; that is, where faster threads have to wait for slower ones.
- The **PARALLEL DO** directive automatically puts an invisible, implied barrier at the end of its **DO** loop:

**!\$OMP PARALLEL DO** 

- DO index = 1, length
  - ... parallel stuff ...

END DO

! Implied barrier

... serial stuff ...

## OpenMP also has an explicit **BARRIER** directive, but most people don't need it.



#### **Critical Sections**

- A *critical section* is a piece of code that any thread can execute, but that only one thread can execute at a time.
- **!\$OMP PARALLEL DO** 
  - DO index = 1, length
    - ... parallel stuff ...
- !\$OMP CRITICAL(summing)

```
sum = sum + x(index) * y(index)
```

- !\$OMP END CRITICAL(summing)
  - ... more parallel stuff ...

END DO

#### What's the point?



#### **Why Have Critical Sections?**

If only one thread at a time can execute a critical section, that slows the code down, because the other threads may be waiting to enter the critical section.
But, for certain statements, if you don't ensure <u>mutual</u> exclusion, then you can get nondeterministic results.



### **If No Critical Section**

```
!$OMP CRITICAL(summing)
```

```
sum = sum + x(index) * y(index)
!$OMP END CRITICAL(summing)
```

## Suppose for thread #0, index is 27, and for thread #1, index is 92.

- If the two threads execute the above statement at the same time, **sum** could be
- the value after adding x(27)\*y(27), or
- the value after adding x(92)\*y(92), or
- garbage!

## This is called a *race condition*: the result depends on who wins the race.



#### Reductions

- A *reduction* converts an array to a scalar: sum, product, minimum value, maximum value, location of minimum value, location of maximum value, Boolean AND, Boolean OR, number of occurrences, etc.
- Reductions are so common, and so important, that OpenMP has a specific construct to handle them: the **REDUCTION** clause in a **PARALLEL DO** directive.



#### **Reduction Clause**

```
total_mass = 0
!$OMP PARALLEL DO REDUCTION(+:total_mass)
D0 index = 1, length
   total_mass = total_mass + mass(index)
END D0 !! index = 1, length
```

#### This is equivalent to:

```
total_mass = 0
D0 thread = 0, number_of_threads - 1
    thread_mass(thread) = 0
END D0
$OMP PARALLEL D0
D0 index = 1, length
    thread = omp_get_thread_num()
    thread_mass(thread) = thread_mass(thread) + mass(index)
END D0 !! index = 1, length
D0 thread = 0, number_of_threads - 1
    total_mass = total_mass + thread_mass(thread)
END D0
```



#### **Parallelizing a Serial Code #1**

#### PROGRAM big\_science

... declarations ...

DO ... ... parallelizable work ... END DO ... serial work ...

DO ... ... more parallelizable work ... END DO ... serial work ... ... etc ... END PROGRAM big science PROGRAM big\_science
... declarations ...
!\$OMP PARALLEL DO ...
DO ...
DO ...
... parallelizable work ...
END DO
... serial work ...
!\$OMP PARALLEL DO ...
DO ...
DO ...
... more parallelizable work ...
END DO
... serial work ...
END PROGRAM big\_science

This way may have lots of **synchronization** overhead.



#### **Parallelizing a Serial Code #2**

#### PROGRAM big\_science

... declarations ...

DO task = 1, numtasks CALL science\_task(...) END DO END PROGRAM big\_science SUBROUTINE science\_task (...) ... parallelizable work ...

... serial work ...

... more parallelizable work ...

... serial work ...

... etc ... END PROGRAM big\_science **PROGRAM** big science ... declarations ... **!\$OMP PARALLEL DO ...** DO task = 1, numtasks CALL science task(...) END DO END PROGRAM big\_science SUBROUTINE science task ( ... ) ... parallelizable work ... **!SOMP MASTER** ... serial work ... **!\$OMP END MASTER** ... more parallelizable work ... **!**SOMP MASTER ... serial work ... **!**SOMP END MASTER ... etc ... END PROGRAM big\_science





#### Part VI: Distributed Multiprocessing



#### References

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