Supercomputing in Plain English



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Tuesday May 1 2018











This is an experiment!

It's the nature of these kinds of videoconferences that FAILURES ARE GUARANTEED TO HAPPEN! NO PROMISES!

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PLEASE MUTE YOURSELF

No matter how you connect, **PLEASE MUTE YOURSELF**, so that we cannot hear you.

At OU, we will turn off the sound on all conferencing technologies.

That way, we won't have problems with **echo cancellation**.

Of course, that means we cannot hear questions.

So for questions, you'll need to send e-mail:

supercomputinginplainenglish@gmail.com

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Download the Slides Beforehand

Before the start of the session, please download the slides from the Supercomputing in Plain English website:

http://www.oscer.ou.edu/education/

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That way, if anything goes wrong, you can still follow along with just audio.

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Zoom

Go to:

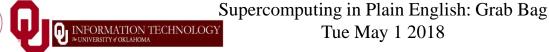
http://zoom.us/j/979158478

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Many thanks Eddie Huebsch, OU CIO, for providing this.

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YouTube

You can watch from a Windows, MacOS or Linux laptop or an Android or iOS handheld using YouTube.

Go to YouTube via your preferred web browser or app, and then search for:

Supercomputing InPlainEnglish

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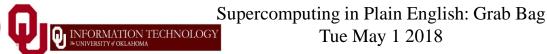
(InPlainEnglish is all one word.)

Many thanks to Skyler Donahue of OneNet for providing this.

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Twitch

You can watch from a Windows, MacOS or Linux laptop or an Android or iOS handheld using Twitch.

Go to:

http://www.twitch.tv/sipe2018

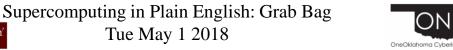
Many thanks to Skyler Donahue of OneNet for providing this.

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Wowza #1

You can watch from a Windows, MacOS or Linux laptop using Wowza from the following URL:

http://jwplayer.onenet.net/streams/sipe.html

If that URL fails, then go to:

http://jwplayer.onenet.net/streams/sipebackup.html

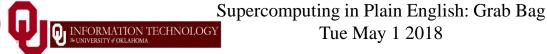
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Many thanks to Skyler Donahue of OneNet for providing this.

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Wowza #2

Wowza has been tested on multiple browsers on each of:

- Windows 10: IE, Firefox, Chrome, Opera, Safari
- MacOS: Safari, Firefox
- Linux: Firefox, Opera

We've also successfully tested it via apps on devices with:

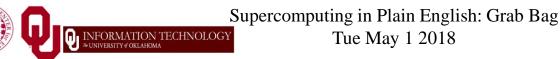
- Android
- iOS

Many thanks to Skyler Donahue of OneNet for providing this.

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Toll Free Phone Bridge

IF ALL ELSE FAILS, you can use our US TOLL phone bridge:

405-325-6688

684 684 #

NOTE: This is for **US** call-ins **ONLY**.

PLEASE MUTE YOURSELF and use the phone to listen.

Don't worry, we'll call out slide numbers as we go.

Please use the phone bridge **ONLY IF** you cannot connect any other way: the phone bridge can handle only 100 simultaneous connections, and we have over 1000 participants.

Many thanks to OU CIO Eddie Huebsch for providing the phone bridge.









Please Mute Yourself

No matter how you connect, **PLEASE MUTE YOURSELF**, so that we cannot hear you.

(For YouTube, Twitch and Wowza, you don't need to do that, because the information only goes from us to you, not from you to us.)

At OU, we will turn off the sound on all conferencing technologies.

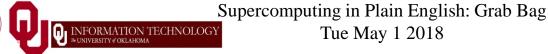
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Of course, that means we cannot hear questions.

So for questions, you'll need to send e-mail.









Questions via E-mail Only

Ask questions by sending e-mail to:

supercomputinginplainenglish@gmail.com

All questions will be read out loud and then answered out loud.

DON'T USE CHAT OR VOICE FOR QUESTIONS!

No one will be monitoring any of the chats, and if we can hear your question, you're creating an **echo cancellation** problem.

PLEASE MUTE YOURSELF. PLEASE MUTE YOURSELF.







Onsite: Talent Release Form

If you're attending onsite, you **MUST** do one of the following:

complete and sign the Talent Release Form,

OR

 sit behind the cameras (where you can't be seen) and don't talk at all.

If you aren't onsite, then PLEASE MUTE YOURSELF.







TENTATIVE Schedule

Tue Jan 23: Storage: What the Heck is Supercomputing?

Tue Jan 30: The Tyranny of the Storage Hierarchy Part I

Tue Feb 6: The Tyranny of the Storage Hierarchy Part II

Tue Feb 13: Instruction Level Parallelism

Tue Feb 20: Stupid Compiler Tricks

Tue Feb 27: Multicore Multithreading

Tue March 6: Distributed Multiprocessing

Tue March 13: NO SESSION (Henry business travel)

Tue March 20: **NO SESSION** (OU's Spring Break)

Tue March 27: Applications and Types of Parallelism

Tue Apr 3: Multicore Madness

Tue Apr 10: **NO SESSION** (Henry business travel)

Tue Apr 17: High Throughput Computing

Tue Apr 24: GPU: Number Crunching in Your Graphics Card

Tue May 1: Grab Bag: Scientific Libraries, I/O Libraries, Visualization











Thanks for helping!

OU IT

- OSCER operations staff (Dave Akin, Patrick Calhoun, Kali McLennan, Jason Speckman, Brett Zimmerman)
- OSCER Research Computing Facilitators (Jim Ferguson, Horst Severini)
- Debi Gentis, OSCER Coordinator
- Kyle Dudgeon, OSCER Manager of Operations
- Ashish Pai, Managing Director for Research IT Services
- The OU IT network team
- OU CIO Eddie Huebsch
- OneNet: Skyler Donahue
- Oklahoma State U: Dana Brunson









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Coming in 2018!

Linux Clusters Institute workshops

http://www.linuxclustersinstitute.org/workshops/

- Introductory HPC Cluster System Administration: May 14-18 2018 @ U Nebraska, Lincoln NE USA
- Intermediate HPC Cluster System Administration: Aug 13-17 2018 @ Yale U, New Haven CT USA
- Great Plains Network Annual Meeting: details coming soon
- Advanced Cyberinfrastructure Research & Education Facilitators (ACI-REF) Virtual Residency Aug 5-10 2018, U Oklahoma, Norman OK USA
- PEARC 2018, July 22-27, Pittsburgh PA USA

https://www.pearc18.pearc.org/

IEEE Cluster 2018, Sep 10-13, Belfast UK

https://cluster2018.github.io

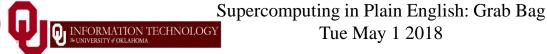
OKLAHOMA SUPERCOMPUTING SYMPOSIUM 2018, Sep 25-26 2018 @ OU

Tue May 1 2018

SC18 supercomputing conference, Nov 11-16 2018, Dallas TX USA

http://sc18.supercomputing.org/







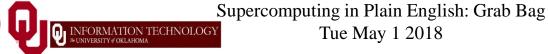


Outline

Tue May 1 2018

- Scientific Computing Pipeline
- Scientific Libraries
- I/O Libraries
- Scientific Visualization









Scientific Computing Pipeline

Real World

Physics

Mathematical Representation (continuous)

Numerical Representation (discrete)

Algorithm

Implementation (program)

Port (to a specific platform)

Result (run)

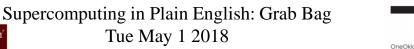
Analysis

Verification

Thanks to Julia Mullen of MIT Lincoln Lab for this concept.









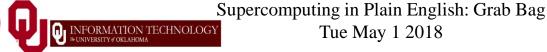
Five Rules of Scientific Computing

Tue May 1 2018

- Know the physics.
- Control the software.
- Understand the numerics.
- Achieve expected behavior.
- Question unexpected behavior.

Thanks to Robert E. Peterkin for these.









Scientific Libraries



Preinvented Wheels

Many simulations perform fairly common tasks; for example, solving systems of equations:

$$Ax = b$$

where A is the matrix of coefficients, x is the vector of unknowns and b is the vector of knowns.

$$\begin{bmatrix} a_{1,1} & a_{1,2} & a_{1,3} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & a_{2,3} & \cdots & a_{2,n} \\ a_{3,1} & a_{3,2} & a_{3,3} & \cdots & a_{3,n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ a_{n,1} & a_{n,2} & a_{n,3} & \cdots & a_{n,n} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ \vdots \\ b_n \end{bmatrix}$$









Scientific Libraries

Because some tasks are quite common across many science and engineering applications, groups of researchers have put a lot of effort into writing *scientific libraries*: collections of routines for performing these commonly-used tasks (for example, linear algebra solvers).

The people who write these libraries know a lot more about these things than we do.

So, a good strategy is to use their libraries, instead of trying to write our own.









Solver Libraries

Probably the most common scientific computing task is solving a system of equations

$$\mathbf{A}\mathbf{x} = \mathbf{b}$$

where **A** is a matrix of coefficients, **x** is a vector of unknowns, and **b** is a vector of knowns.

The goal is to solve for \mathbf{x} .





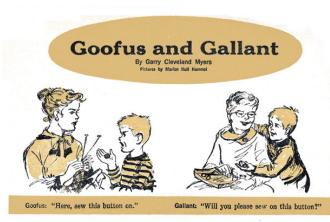


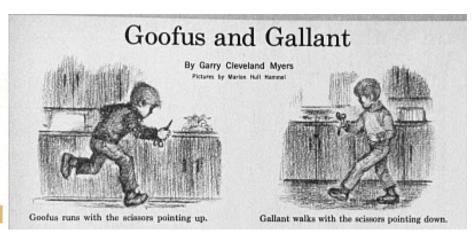


Solving Systems of Equations

Don'ts:

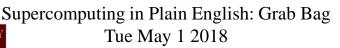
- **Don't** invert the matrix $(\mathbf{x} = \mathbf{A}^{-1}\mathbf{b})$. That's much more costly than solving directly, and much more prone to numerical error.
- Don't write your own solver code. There are people who devote their whole careers to writing solvers.
 They know a lot more about writing solvers than we do.











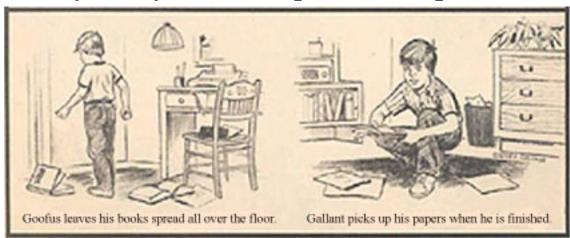


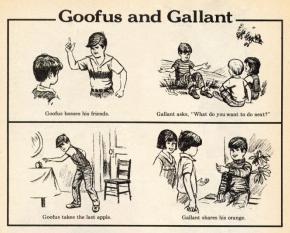


Solving Do's

Do's:

- **Do** use standard, portable solver libraries.
- Do use a version that's tuned for the platform that you're running on, if available.
- Do use the information that you have about your system of equations to pick the most efficient solver.









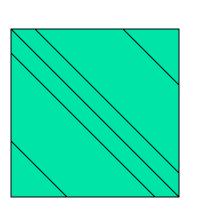


All About Your Matrix

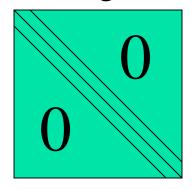
If you know things about your matrix, you might be able to use a more efficient solver.

- Symmetric: $a_{i,j} = a_{j,i}$
- Positive definite: $\mathbf{x}^T \mathbf{A} \mathbf{x} > 0$ for all $\mathbf{x} \neq 0$ (for example, if all eigenvalues are positive)
- Banded:

zero
except
on the
bands



Tridiagonal:



and ...

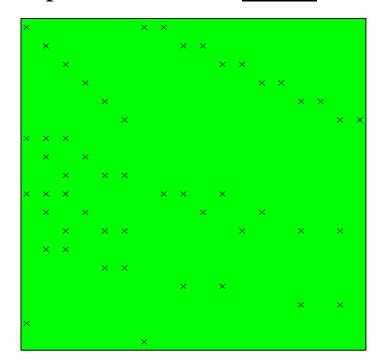






Sparse Matrices

A <u>sparse matrix</u> is a matrix that has mostly zeros in it. "Mostly" is vaguely defined, but a good rule of thumb is that a matrix is sparse if more than, say, 90-95% of its entries are zero. (A non-sparse matrix is <u>dense</u>.)











Linear Algebra Libraries

- BLAS [1],[2]
- ATLAS^[3]
- LAPACK^[4]
- ScaLAPACK^[5]
- PETSc^{[6],[7],[8]}









BLAS

The Basic Linear Algebra Subprograms (BLAS) are a collection of low-level linear algebra routines:

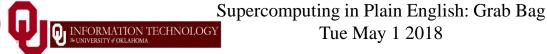
- Level 1: Vector-vector (for example, dot product)
- Level 2: Matrix-vector (for example, matrix-vector multiply)
- Level 3: Matrix-matrix (for example, matrix-matrix multiply)

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Many linear algebra packages, including LAPACK, ScaLAPACK and PETSc, are built on top of BLAS.

Most supercomputer vendors have versions of BLAS that are highly tuned for their platforms.









ATLAS

The <u>Automatically Tuned Linear Algebra Software</u> package (ATLAS) is a self-tuned version of BLAS (it also includes a few LAPACK routines).

When it's installed, it tests and times a variety of approaches to each routine, and selects the version that runs the fastest.

ATLAS is substantially faster than the generic version of BLAS. And, it's **FREE**!









Goto BLAS

Several years ago, a new version of BLAS was released, developed by Kazushige Goto (then at UT Austin, now at Intel).

http://en.wikipedia.org/wiki/Kazushige_Goto

This version is unusual, because instead of optimizing for cache, it optimizes for the *Translation Lookaside Buffer* (TLB), the special little cache that often is ignored by software developers.

Goto realized that optimizing for the TLB would be more efficient than optimizing for cache.









Platform-specific BLAS

- Many platforms have their own version of BLAS that's highly tuned for that platform:
 - Intel Math Kernel Library*
 - AMD Core Math Library*
 - IBM Engineering & Scientific Subroutine Library*
 - Oracle Sun Performance Library*
 - cuBLAS
- * Includes routines other than BLAS.

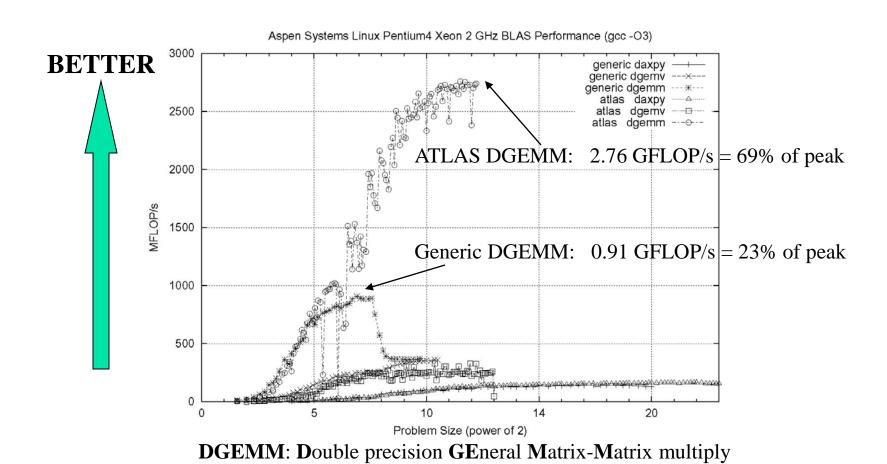








ATLAS vs. Generic BLAS



DGEMV: Double precision GEneral Matrix-Vector multiply
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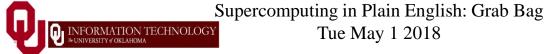
LAPACK

- **LAPACK** (Linear Algebra PACKage) solves dense or specialcase sparse systems of equations depending on matrix properties such as:
- Precision: single, double
- Data type: real, complex
- Shape: diagonal, bidiagonal, tridiagonal, banded, triangular, trapezoidal, Hesenberg, general dense

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- Properties: orthogonal, positive definite, Hermetian (complex), symmetric, general
- LAPACK is built on top of BLAS, which means it can benefit from tuned BLAS version.









LAPACK Example

```
REAL, DIMENSION (numrows, numcols) ::
REAL, DIMENSION (numrows)
REAL, DIMENSION (numcols)
INTEGER,DIMENSION(numrows)
INTEGER :: row, col, info, numrhs = 1
DO row = 1, numrows
  B(row) = ...
END DO
DO col = 1, numcols
  DO row = 1, numrows
    A(row,col) = ...
  END DO
END DO
CALL sgesv(numrows, numrhs, A, numrows, pivot, &
           B, numrows, info)
DO col = 1, numcols
  X(col) = B(col)
END DO
```







LAPACK: A Library and an API

LAPACK is a library that you can download for free from the Web:

www.netlib.org

But, it's also an Application Programming Interface (API): a definition of a set of routines, their arguments, and their behaviors.

So, anyone can write an implementation of LAPACK.









It's Good to Be Popular

LAPACK is a good choice for non-parallelized solving, because its popularity has convinced many supercomputer vendors to write their own, highly tuned versions.

The API for the LAPACK routines is the same as the portable version from NetLib, but the performance can be much better, via either ATLAS or proprietary vendor-tuned versions.

Also, some vendors have shared memory parallel versions of LAPACK.









LAPACK Performance

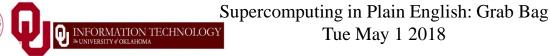
Because LAPACK uses BLAS, it's about as fast as BLAS.

For example, DGESV (Double precision General SolVer) on a 2 GHz Pentium4 using ATLAS gets 65% of peak, compared to 69% of peak for Matrix-Matrix multiply.

In fact, an older version of LAPACK, called LINPACK, is used to determine the top 500 supercomputers in the world.

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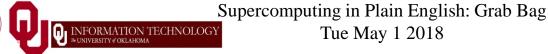
ScaLAPACK

ScaLAPACK is the distributed parallel (MPI) version of LAPACK. It actually contains only a subset of the LAPACK routines, and has a somewhat awkward Application Programming Interface (API).

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Like LAPACK, ScaLAPACK is also available from www.netlib.org.









PETSc

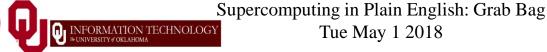
PETSc (Portable, Extensible Toolkit for Scientific Computation) is a solver library for sparse matrices that uses distributed parallelism (MPI).

PETSc is designed for general sparse matrices with no special properties, but it also works well for sparse matrices with simple properties like banding and symmetry.

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It has a simpler, more intuitive Application Programming Interface than ScaLAPACK.









Pick Your Solver Package

- Dense Matrix
 - Serial: LAPACK
 - Shared Memory Parallel: threaded LAPACK
 - Distributed Parallel: ScaLAPACK
- Sparse Matrix: PETSc









I/O Libraries



I/O Challenges

I/O presents two important challenges to scientific computing:

- Performance
- Portability

The performance issue arises because I/O is much more timeconsuming than computation, as we saw in the "Storage Hierarchy" session.

The portability issue arises because different kinds of computers can have different ways of representing real (floating point) numbers.









Storage Formats

When you use a **PRINT** statement in Fortran or a **printf** in C or output to **cout** in C++, you are asking the program to output data in human-readable form:

$$x = 5$$
PRINT *, x

But what if the value that you want to output is a real number with lots of significant digits?









Data Output as Text

1.3456789E+23

When you output data as text, each character takes 1 byte.

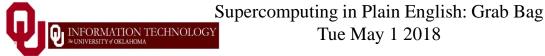
So if you output a number with lots of digits, then you're outputting lots of bytes.

For example, the above number takes 13 bytes to output as text.

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Jargon: Text is sometimes called **ASCII** (American Standard Code for Information Interchange).









Output Data in Binary

Inside the computer, a single precision real number (Fortran REAL, C/C++ float) typically requires 4 bytes, and a double precision real number (DOUBLE PRECISION or double) typically requires 8.

That's less than 13 bytes.

Since I/O is very expensive, it's better to output 4 or 8 bytes than 13 or more.

Happily, Fortran, C and C++ allow you to output data as **binary** (internal representation) rather than as text.









Binary Output Problems

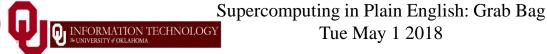
When you output data as **binary** rather than as text, you output substantially **fewer bytes**, so you save time (because I/O is very expensive) and you save disk space.

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But, you pay two prices:

- **Readability**: Humans can't read binary.
- **Portability**: Different kinds of computers have different ways of internally representing numbers.









Binary Readability: No Problem

Readability of binary data **isn't a problem** in scientific computing, because:

- You can always write a little program to read in the binary data and display its text equivalent.
- If you have lots and lots of data (that is, MBs or GBs), you wouldn't want to look at all of it anyway.







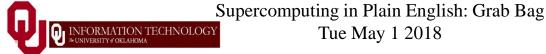
Binary Portability: Big Problem

Binary data portability is a very big problem in scientific computing, because data that's output on one kind of computer may not be readable on another, and so:

- You can't output the data on one kind of computer and then use them (for example, visualize, analyze) on another kind.
- Some day the kind of computer that output the data will be obsolete, so there may be no computer in the world that can input it, and thus the data are lost.

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Portable Binary Data

The HPC community noticed this problem some years ago, and so a number of portable binary data formats were developed. The two most popular are:

■ <u>HDF</u> (Hierarchical Data Format) from the National Center for Supercomputing Applications:

http://www.hdfgroup.org/

NetCDF (Network Common Data Form) from Unidata:

http://www.unidata.ucar.edu/software/netcdf









Advantages of Portable I/O

Portable binary I/O packages:

- give you portable binary I/O;
- have simple, clear APIs;
- are available for <u>free;</u>
- run on most platforms;
- allow you to <u>annotate</u> your data (for example, put into the file the variable names, units, experiment name, grid description, etc).

Also, both HDF and netCDF support distributed parallel I/O.







Scientific Visualization



Too Many Numbers

'A typical scientific code outputs lots and lots of data.

For example, the ARPS weather forecasting code, running a 5 day forecast over the continental U.S. with a resolution of 1 km horizontal and 0.25 km vertical outputting data for every hour would produce about **10 terabytes** (10¹³ bytes).

No one can look at that many numbers.

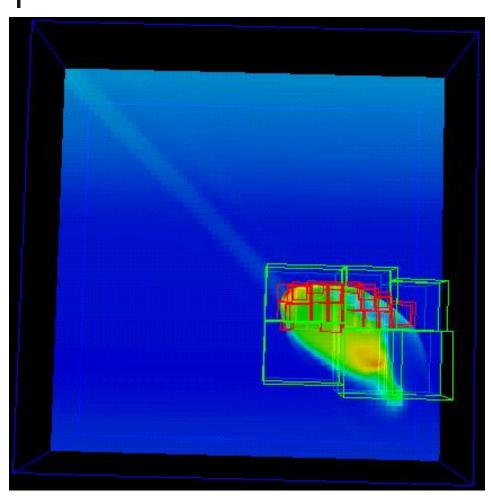








A Picture is Worth ...



... millions of numbers.

This is Comet Shoemaker-Levy 9, which hit Jupiter in 1994; the image is from 35 seconds after hitting Jupiter's inner atmosphere.^[9]









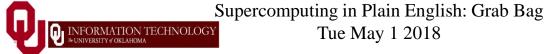
Types of Visualization

- Contour lines
- Slice planes
- Isosurfaces
- **Streamlines**
- Volume rendering
- ... and many others.

Note: Except for the volume rendering, the following images were created by Vis5D.[10]

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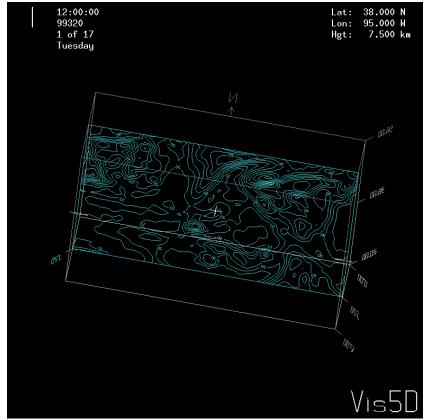






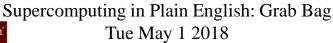
Contour Lines

This image shows *contour lines* of relative humidity. Each contour line represents a single humidity value.





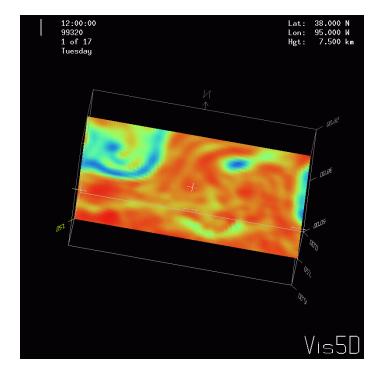






Slice Planes

A <u>slice plane</u> is a single plane passed through a 3D volume. Typically, it is color coded by mapping some scalar variable to color (for example, low vorticity to blue, high vorticity to red).





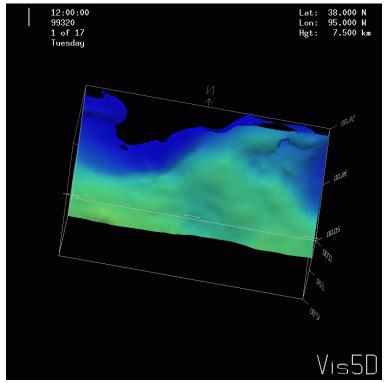


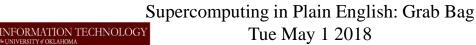




Isosurfaces

An <u>isosurface</u> is a surface that has a constant value for some scalar quantity. This image shows an isosurface of temperature at 0° Celsius, colored with pressure.



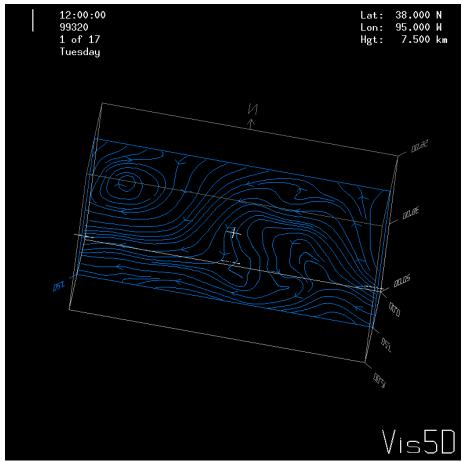






Streamlines

A streamline traces a vector quantity (for example, velocity).







Supercomputing in Plain English: Grab Bag

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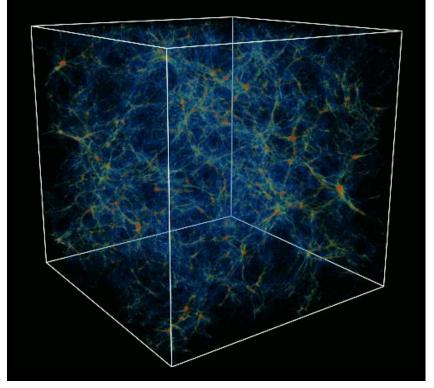


Volume Rendering

A *volume rendering* is created by mapping some variable (for example, energy) to color and another variable (for

example, density) to opacity.

This image shows the overall structure of the universe.^[11]
Notice that the image looks like thick colored smoke.









Thanks for your attention!

Q

Questions?

www.oscer.ou.edu



Thanks for helping!

OU IT

- OSCER operations staff (Dave Akin, Patrick Calhoun, Kali McLennan, Jason Speckman, Brett Zimmerman)
- OSCER Research Computing Facilitators (Jim Ferguson, Horst Severini)
- Debi Gentis, OSCER Coordinator
- Kyle Dudgeon, OSCER Manager of Operations
- Ashish Pai, Managing Director for Research IT Services
- The OU IT network team
- OU CIO Eddie Huebsch
- OneNet: Skyler Donahue
- Oklahoma State U: Dana Brunson









This is an experiment!

It's the nature of these kinds of videoconferences that FAILURES ARE GUARANTEED TO HAPPEN! NO PROMISES!

So, please bear with us. Hopefully everything will work out well enough.

If you lose your connection, you can retry the same kind of connection, or try connecting another way.

Remember, if all else fails, you always have the phone bridge to fall back on.

PLEASE MUTE YOURSELF.

PLEASE MUTE YOURSELF.

PLEASE MUTE YOURSELF.







Coming in 2018!

Linux Clusters Institute workshops

http://www.linuxclustersinstitute.org/workshops/

- Introductory HPC Cluster System Administration: May 14-18 2018 @ U Nebraska, Lincoln NE USA
- Intermediate HPC Cluster System Administration: Aug 13-17 2018 @ Yale U, New Haven CT USA
- Great Plains Network Annual Meeting: details coming soon
- Advanced Cyberinfrastructure Research & Education Facilitators (ACI-REF) Virtual Residency Aug 5-10 2018, U Oklahoma, Norman OK USA
- PEARC 2018, July 22-27, Pittsburgh PA USA

https://www.pearc18.pearc.org/

IEEE Cluster 2018, Sep 10-13, Belfast UK

https://cluster2018.github.io

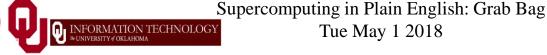
OKLAHOMA SUPERCOMPUTING SYMPOSIUM 2018, Sep 25-26 2018 @ OU

Tue May 1 2018

SC18 supercomputing conference, Nov 11-16 2018, Dallas TX USA

http://sc18.supercomputing.org/









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- [10] http://www.ssec.wisc.edu/~billh/vis5d.html
- [11] Image by Greg Bryan, MIT.





