Supercomputing in Plain English Grab Bag: Scientific Libraries, I/O Libraries, Visualization

Henry Neeman, Director

OU Supercomputing Center for Education & Research University of Oklahoma Information Technology Tuesday May 3 2011





This is an experiment!

It's the nature of these kinds of videoconferences that FAILURES ARE GUARANTEED TO HAPPEN! NO PROMISES!

- So, please bear with us. Hopefully everything will work out well enough.
- If you lose your connection, you can retry the same kind of connection, or try connecting another way.
- Remember, if all else fails, you always have the toll free phone bridge to fall back on.





Access Grid

If you aren't sure whether you have AG, you probably don't.

Tue May 3	Helium

Many thanks to Patrick Calhoun of OU for setting these up for us.





H.323 (Polycom etc)

From an H.323 device (e.g., <u>Polycom</u>, <u>Tandberg</u>, <u>Lifesize</u>, etc):

- If you ARE already registered with the <u>OneNet</u> gatekeeper: Dial
 2500409
- If you **AREN'T** registered with the <u>OneNet</u> gatekeeper (probably the case):
 - Dial: 164.58.250.47
 - 2. Bring up the virtual keypad.
 On some H.323 devices, you can bring up the virtual keypad by typing:
 #
 - When asked for the conference ID, enter: 0409
 - 4. On some H.323 devices, you indicate the end of conference ID with:
 #

Many thanks to Roger Holder and OneNet for providing this.





H.323 from Internet Explorer

From a Windows PC running Internet Explorer:

- 1. You **MUST** have the ability to install software on the PC (or have someone install it for you).
- 2. Download and install the latest Java Runtime Environment (JRE) from here: <u>http://www.oracle.com/technetwork/java/javase/downloads/</u> (Click on the Java Download icon, because that install package includes both the JRE and other components.)
- Download and install this video decoder: <u>http://164.58.250.47/codian video decoder.msi</u>
- 4. Start Internet Explorer.
- 5. Copy-and-paste this URL into your IE window: http://164.58.250.47/
- 6. When that webpage loads, in the upper left, click on "Streaming."
- 7. In the textbox labeled Sign-in Name, type your name.
- In the textbox labeled Conference ID, type this: 0409
- 9. Click on "Stream this conference."
- 10. When that webpage loads, you may see, at the very top, a bar offering you options. If so, click on it and choose "Install this add-on."





H.323 from XMeeting (MacOS)

From a Mac running MacOS X:

- 1. Download XMeeting from http://xmeeting.sourceforge.net/
- 2. Install XMeeting as follows:
 - a. Open the .dmg file.
 - b. Drag XMeeting into the Applications folder.
- 3. Open XMeeting from Applications.
- 4. Skip the setup wizard.
- 5. In the call box, type **164.58.250.47**
- 6. Click the **Call** button.
- From the Remote Control window, when prompted to join the conference, enter : 0409#







There's a quick tutorial on the OSCER education webpage.





QuickTime Broadcaster

If you cannot connect via the Access Grid, H.323 or EVO, then you can connect via QuickTime:

rtsp://129.15.254.141/test_hpc09.sdp

We recommend using QuickTime Player for this, because we've tested it successfully.

We recommend upgrading to the latest version at:

http://www.apple.com/quicktime/

When you run QuickTime Player, traverse the menus

File -> Open URL

Then paste in the rstp URL into the textbox, and click OK. Many thanks to Kevin Blake of OU for setting up QuickTime Broadcaster for us.







We have only a limited number of WebEx connections, so please avoid WebEx unless you have **<u>NO OTHER WAY</u>** <u>**TO CONNECT**</u>.

Instructions are available on the OSCER education webpage.

Thanks to Tim Miller of Wake Forest U.





Phone Bridge

If all else fails, you can call into our toll free phone bridge: US: 1-800-832-0736, *6232874# International: 303-330-0440, *6232874# Please mute yourself and use the phone to listen. Don't worry, we'll call out slide numbers as we go. Please use the phone bridge **ONLY** if you cannot connect any other way: the phone bridge is charged per connection per minute, so our preference is to minimize the number of connections.

Many thanks to Amy Apon and U Arkansas for providing the previous toll free phone bridge.





No matter how you connect, please mute yourself, so that we cannot hear you.

- At OU, we will turn off the sound on all conferencing technologies.
- That way, we won't have problems with echo cancellation.
- Of course, that means we cannot hear questions.
- So for questions, you'll need to send some kind of text.





Questions via Text: E-mail

Ask questions via e-mail to **sipe2011@yahoo.com**.

All questions will be read out loud and then answered out loud.





Thanks for helping!

- OSCER operations staff: Brandon George, Dave Akin, Brett Zimmerman, Josh Alexander
- Horst Severini, OSCER Associate Director for Remote & Heterogeneous Computing
- OU Research Campus staff (Patrick Calhoun, Mark McAvoy)
- Kevin Blake, OU IT (videographer)
- John Chapman, Jeff Pummill and Amy Apon, U Arkansas
- James Deaton and Roger Holder, OneNet
- Tim Miller, Wake Forest U
- Jamie Hegarty Schwettmann, i11 Industries





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Supercomputing Exercises

Want to do the "Supercomputing in Plain English" exercises?

- The first exercise is already posted at: http://www.oscer.ou.edu/education.php
- If you don't yet have a supercomputer account, you can get a temporary account, just for the "Supercomputing in Plain English" exercises, by sending e-mail to:

hneeman@ou.edu

Please note that this account is for doing the <u>exercises only</u>, and will be shut down at the end of the series.

• The Grab Bag exercise has been posted.





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OK Supercomputing Symposium 2011



2003 Keynote: Peter Freeman NSF Computer & Information Science & Engineering Assistant Director



2004 Keynote: Sangtae Kim NSF Shared Cyberinfrastructure Division Director



2005 Keynote: Walt Brooks NASA Advanced Supercomputing Division Director



2006 Keynote:
Dan Atkins2007 Keynote:
Jay BoisseaudHead of NSF's
Office ofDirector
Texas AdvancedorCyberinfrastructureComputing Center
U. Texas Austin



2008 Keynote: José Munoz Deputy Office Director/ Senior Scientific Advisor NSF Office of Cyberinfrastructure



2009 Keynote: Douglass Post Chief Scientist US Dept of Defense HPC Modernization Program

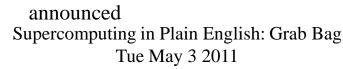


2010 Keynote: Horst Simon Deputy Director Lawrence Berkeley National Laboratory





2011 Keynote to be



FREE! Wed Oct 12 2011 @ OU

http://symposium2011.oscer.ou.edu/

Parallel Programming Workshop FREE! Tue Oct 11 2011 @ OU FREE! Symposium Wed Oct 12 2011 @ OU

REGISTRATION IS NOW OPEN!



SC11 Education Program

- At the SC11 supercomputing conference, we'll hold our annual Education Program, Sat Nov 12 Tue Nov 15.
- You can apply to attend, either fully funded by SC11 or self-funded.
- Henry is the SC11 Education Chair.
- We'll alert everyone once the registration website opens.





Outline

- Scientific Computing Pipeline
- Scientific Libraries
- I/O Libraries
- Scientific Visualization



Scientific Computing Pipeline

Real World Physics Mathematical Representation (continuous) Numerical Representation (discrete) Algorithm Implementation (program) Port (to a specific platform) Result (run) Analysis Verification Thanks to Julia Mullen of MIT Lincoln Lab for this concept.



Five Rules of Scientific Computing

- 1. Know the physics.
- 2. Control the software.
- 3. Understand the numerics.
- 4. Achieve expected behavior.
- 5. Question unexpected behavior.

Thanks to Robert E. Peterkin for these.





Scientific Libraries



Preinvented Wheels

Many simulations perform fairly common tasks; for example, solving systems of equations: Ax = b

where **A** is the matrix of coefficients, **x** is the vector of unknowns and **b** is the vector of knowns.

$$\begin{bmatrix} a_{1,1} & a_{1,2} & a_{1,3} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & a_{2,3} & \cdots & a_{2,n} \\ a_{3,1} & a_{3,2} & a_{3,3} & \cdots & a_{3,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n,1} & a_{n,2} & a_{n,3} & \cdots & a_{n,n} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ \vdots \\ b_n \end{bmatrix}$$





Scientific Libraries

Because some tasks are quite common across many science and engineering applications, groups of researchers have put a lot of effort into writing <u>scientific libraries</u>: collections of routines for performing these commonly-used tasks (for example, linear algebra solvers).

The people who write these libraries know a lot more about these things than we do.

So, a good strategy is to use their libraries, rather than trying to write our own.





Solver Libraries

Probably the most common scientific computing task is solving a system of equations Ax = b

where **A** is a matrix of coefficients, **x** is a vector of unknowns, and **b** is a vector of knowns.

The goal is to solve for **x**.

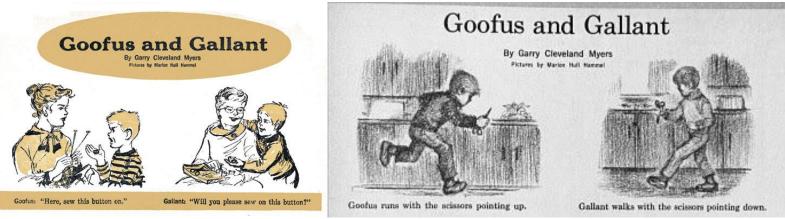


Q

Solving Systems of Equations

Don'ts:

- Don't invert the matrix (x = A⁻¹b). That's much more costly than solving directly, and much more prone to numerical error.
- <u>Don't</u> write your own solver code. There are people who devote their whole careers to writing solvers. They know a lot more about writing solvers than we do.









Do's:

- **Do** use standard, portable solver libraries.
- <u>Do</u> use a version that's tuned for the platform you're running on, if available.
- <u>Do</u> use the information that you have about your system of equations to pick the most efficient solver.





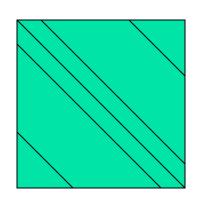


All About Your Matrix

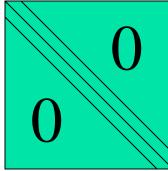
If you know things about your matrix, you maybe can use a more efficient solver.

- Symmetric: $a_{i,j} = a_{j,i}$
- Positive definite: x^TAx > 0 for all x ≠ 0 (for example, if all eigenvalues are positive)
- Banded:

zero except on the bands



Tridiagonal:



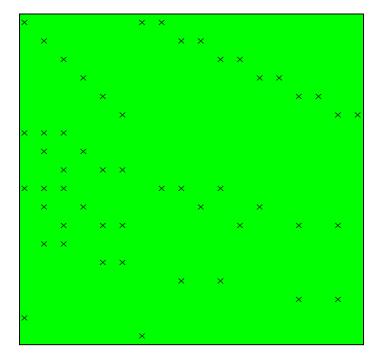
and ...





Sparse Matrices

A <u>sparse matrix</u> is a matrix that has mostly zeros in it. "Mostly" is vaguely defined, but a good rule of thumb is that a matrix is sparse if more than, say, 90-95% of its entries are zero. (A non-sparse matrix is <u>dense</u>.)







Linear Algebra Libraries

- BLAS [1],[2]
- ATLAS^[3]
- LAPACK^[4]
- ScaLAPACK^[5]
- $PETSc^{[6],[7],[8]}$







The **Basic Linear Algebra Subprograms** (BLAS) are a set of low level linear algebra routines:

- Level 1: Vector-vector (for example, dot product)
- Level 2: Matrix-vector (for example, matrix-vector multiply)
- Level 3: Matrix-matrix (for example, matrix-matrix multiply)
- Many linear algebra packages, including LAPACK, ScaLAPACK and PETSc, are built on top of BLAS.
- Most supercomputer vendors have versions of BLAS that are highly tuned for their platforms.







The <u>Automatically Tuned Linear Algebra Software</u> package (ATLAS) is a self-tuned version of BLAS (it also includes a few LAPACK routines).

- When it's installed, it tests and times a variety of approaches to each routine, and selects the version that runs the fastest.
- ATLAS is substantially faster than the generic version of BLAS.

And, it's **FREE**!





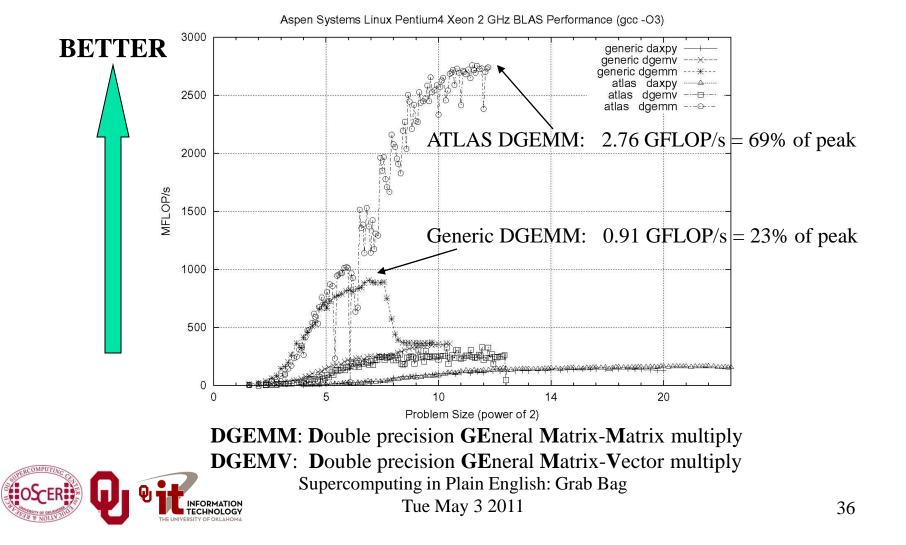


- In the past several years, a new version of BLAS has been released, developed by Kazushige Goto (currently at UT Austin).
- This version is unusual, because instead of optimizing for cache, it optimizes for the *Translation Lookaside Buffer* (TLB), which is a special little cache that often is ignored by software developers.
- Goto realized that optimizing for the TLB would be more efficient than optimizing for cache.





ATLAS vs. Generic BLAS



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LAPACK

LAPACK (Linear Algebra PACKage) solves dense or specialcase sparse systems of equations depending on matrix properties such as:

- Precision: single, double
- Data type: real, complex
- Shape: diagonal, bidiagonal, tridiagonal, banded, triangular, trapezoidal, Hesenberg, general dense
- Properties: orthogonal, positive definite, Hermetian (complex), symmetric, general
- LAPACK is built on top of BLAS, which means it can benefit from ATLAS.





LAPACK Example

```
REAL, DIMENSION (numrows, numcols) :: A
REAL, DIMENSION (numrows)
                                   :: B
                                    : X
REAL, DIMENSION (numcols)
INTEGER, DIMENSION (numrows)
                                   :: pivot
INTEGER :: row, col, info, numrhs = 1
DO row = 1, numrows
  B(row) = \dots
END DO
DO col = 1, numcols
  DO row = 1, numrows
    A(row, col) = ...
  END DO
END DO
CALL sgesv(numrows, numrhs, A, numrows, pivot, &
           B, numrows, info)
&
DO col = 1, numcols
  X(col) = B(col)
END DO
```



LAPACK: A Library and an API

LAPACK is a library that you can download for free from the Web:

www.netlib.org

- But, it's also an Application Programming Interface (API): a definition of a set of routines, their arguments, and their behaviors.
- So, anyone can write an implementation of LAPACK.





It's Good to Be Popular

LAPACK is a good choice for non-parallelized solving, because its popularity has convinced many supercomputer vendors to write their own, highly tuned versions.

- The API for the LAPACK routines is the same as the portable version from NetLib, but the performance can be much better, via either ATLAS or proprietary vendor-tuned versions.
- Also, some vendors have shared memory parallel versions of LAPACK.





LAPACK Performance

Because LAPACK uses BLAS, it's about as fast as BLAS.

- For example, DGESV (Double precision General SolVer) on a 2 GHz Pentium4 using ATLAS gets 65% of peak, compared to 69% of peak for Matrix-Matrix multiply.
- In fact, an older version of LAPACK, called LINPACK, is used to determine the top 500 supercomputers in the world.







ScaLAPACK is the distributed parallel (MPI) version of LAPACK. It actually contains only a subset of the LAPACK routines, and has a somewhat awkward Application Programming Interface (API).

Like LAPACK, ScaLAPACK is also available from

www.netlib.org.







<u>PETSc</u> (Portable, Extensible Toolkit for Scientific Computation) is a solver library for sparse matrices that uses distributed parallelism (MPI).

- PETSc is designed for general sparse matrices with no special properties, but it also works well for sparse matrices with simple properties like banding and symmetry.
- It has a simpler, more intuitive Application Programming Interface than ScaLAPACK.





Pick Your Solver Package

- Dense Matrix
 - Serial: LAPACK
 - Shared Memory Parallel: threaded LAPACK
 - Distributed Parallel: ScaLAPACK
- Sparse Matrix: PETSc





I/O Libraries



I/O Challenges

I/O presents two important challenges to scientific computing:

- Performance
- Portability
- The performance issue arises because I/O is much more timeconsuming than computation, as we saw in the "Storage Hierarchy" session.
- The portability issue arises because different kinds of computers can have different ways of representing real (floating point) numbers.







When you use a **PRINT** statement in Fortran or a **printf** in C or output to **cout** in C++, you are asking the program to output data in human-readable form:

 $\mathbf{x} = 5$

PRINT *, x

But what if the value that you want to output is a real number with lots of significant digits?

1.3456789E+23





Data Output as Text

1.3456789E+23

When you output data as text, each character takes 1 byte.

- So if you output a number with lots of digits, then you're outputting lots of bytes.
- For example, the above number takes 13 bytes to output as text.
- Jargon: Text is sometimes called <u>ASCII</u> (American Standard Code for Information Interchange).





Output Data in Binary

Inside the computer, a single precision real number (Fortran REAL, C/C++ float) typically requires 4 bytes, and a double precision number (DOUBLE PRECISION or double) typically requires 8.

That's less than 13.

- Since I/O is very expensive, it's better to output 4 or 8 bytes than 13 or more.
- Happily, Fortran, C and C++ allow you to output data as **binary** (internal representation) rather than as text.





Binary Output Problems

When you output data as **<u>binary</u>** rather than as text, you output substantially <u>**fewer bytes**</u>, so you save time (since I/O is very expensive) and you save disk space.

But, you pay two prices:

- **<u>Readability</u>**: Humans can't read binary.
- **<u>Portability</u>**: Different kinds of computers have different ways of internally representing numbers.



Binary Readability: No Problem

<u>Readability</u> of binary data <u>isn't a problem</u> in scientific computing, because:

- You can always write a little program to read in the binary data and display its text equivalent.
- If you have lots and lots of data (that is, MBs or GBs), you wouldn't want to look at all of it anyway.



Binary Portability: Big Problem

- **Binary data portability** is a **very big problem** in scientific computing, because data that's output on one kind of computer may not be readable on another, and so:
- You can't output the data on one kind of computer and then use them (for example, visualize, analyze) on another kind.
- Some day the kind of computer that output the data will be obsolete, so there may be no computer in the world that can input it, and thus the data are lost.





Portable Binary Data

The HPC community noticed this problem some years ago, and so a number of portable binary data formats were developed. The two most popular are:

• <u>**HDF**</u> (Hierarchical Data Format) from the National Center for Supercomputing Applications:

http://www.hdfgroup.org/

<u>NetCDF</u> (Network Common Data Form) from Unidata:
 http://www.unidata.ucar.edu/software/netcdf





Advantages of Portable I/O

Portable binary I/O packages:

- give you portable binary I/O;
- have simple, clear APIs;
- are available for <u>free;</u>
- run on most platforms;
- allow you to <u>annotate</u> your data (for example, put into the file the variable names, units, experiment name, grid description, etc).

Also, both HDF and netCDF support distributed parallel I/O.



Q Scientific Visualization



Too Many Numbers

A typical scientific code outputs lots and lots of data.

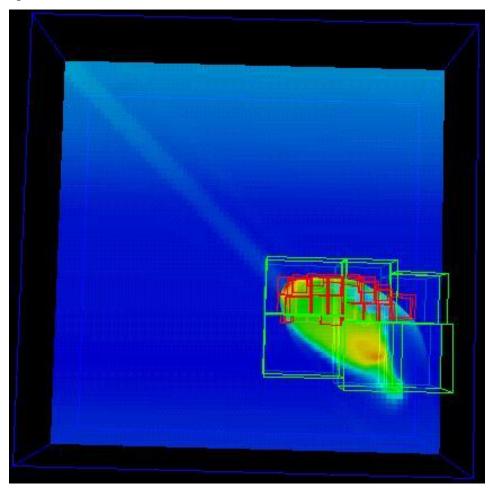
For example, the ARPS weather forecasting code, running a 5 day forecast over the continental U.S. with a resolution of 1 km horizontal and 0.25 km vertical outputting data for every hour would produce about **10 terabytes** (10¹³ bytes).

No one can look at that many numbers.





A Picture is Worth ...



... millions of numbers.

This is Comet Shoemaker-Levy 9, which hit Jupiter in 1994; the image is from 35 seconds after hitting Jupiter's inner atmosphere.^[9]





Types of Visualization

- Contour lines
- Slice planes
- Isosurfaces
- Streamlines
- Volume rendering
- ... and many others.

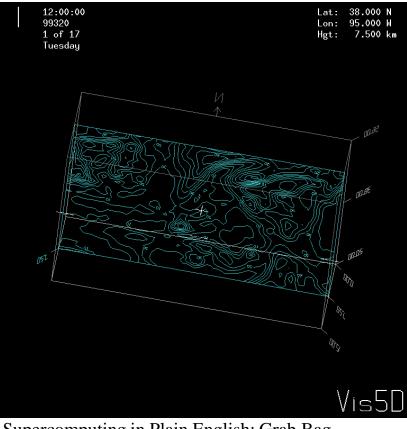
Note: except for the volume rendering, the following images were created by Vis5D,^[10] which you can download for free.





Contour Lines

This image shows *contour lines* of relative humidity. Each contour line represents a single humidity value.

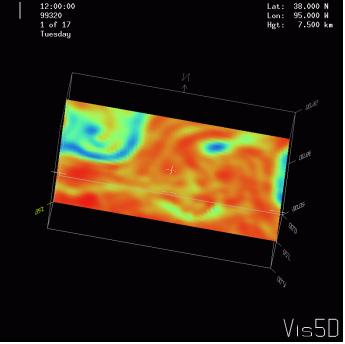








A <u>slice plane</u> is a single plane passed through a 3D volume. Typically, it is color coded by mapping some scalar variable to color (for example, low vorticity to blue, high vorticity to red).

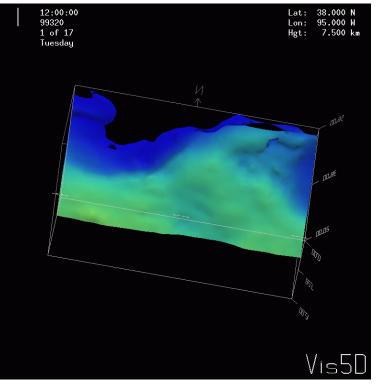






Isosurfaces

An *isosurface* is a surface that has a constant value for some scalar quantity. This image shows an isosurface of temperature at 0° Celsius, colored with pressure.

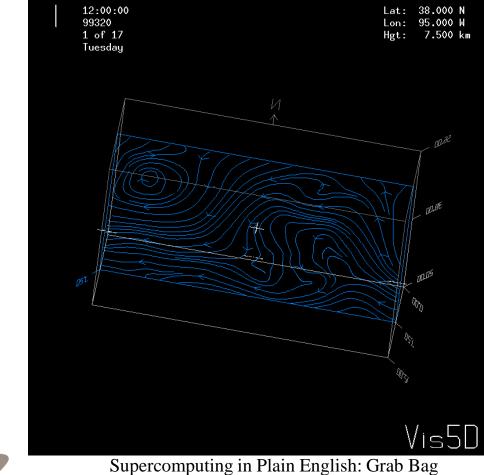






Streamlines

A streamline traces a vector quantity (for example, velocity).



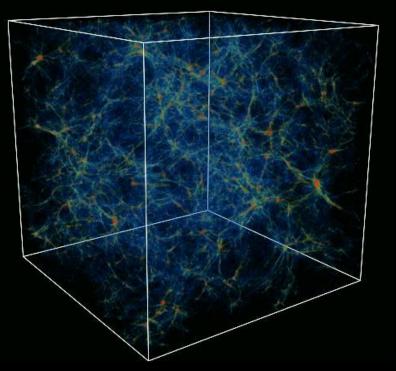




Volume Rendering

A *volume rendering* is created by mapping some variable (for example, energy) to color and another variable (for example, density) to opacity.

This image shows the overall structure of the universe.^[11] Notice that the image looks like thick colored smoke.







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2006 Keynote: 2007 Keynote: Dan Atkins Jay Boisseau Head of NSF's Director Office of **Texas Advanced** Cyberinfrastructure Computing Center U. Texas Austin



2008 Keynote: José Munoz Deputy Office Director/ Senior Scientific Advisor NSF Office of Cyberinfrastructure



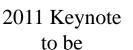
2009 Keynote: **Douglass Post Chief Scientist** US Dept of Defense **HPC** Modernization Program

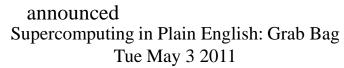


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References

[1] C. L. Lawson, R. J. Hanson, D. Kincaid, and F. T. Krogh, *Basic Linear Algebra Subprograms for FORTRAN* Usage, <u>ACM Trans. Math. Soft., 5 (1979)</u>, pp. 308--323.

[2] http://www.netlib.org/blas/

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- [4] E. Anderson, Z. Bai, C. Bischof, S. Blackford, J. Demmel, J. Dongarra, J. Du Croz, A. Greenbaum, S. Hammarling, A. McKenney, D. Sorensen, *LAPACK Users' Guide*, 3rd ed, 1999. <u>http://www.netlib.org/lapack/</u>
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