Parallel Programming & Cluster Computing

Shared Memory Parallelism

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Outline

- Parallelism
- Shared Memory Parallelism
- OpenMP
Parallelism
Parallelism

Parallelism means doing multiple things at the same time: you can get more work done in the same amount of time.

Less fish …

More fish!
What Is Parallelism?

Parallelism is the use of multiple processing units – either processors or parts of an individual processor – to solve a problem, and in particular the use of multiple processing units operating concurrently on different parts of a problem. The different parts could be different tasks, or the same task on different pieces of the problem’s data.
Kinds of Parallelism

- Shared Memory Multithreading (our topic today)
- Distributed Memory Multiprocessing (next time)
- Hybrid Shared/Distributed
Why Parallelism Is Good

- **The Trees**: We like parallelism because, as the number of processing units working on a problem grows, we can solve **the same problem in less time**.
- **The Forest**: We like parallelism because, as the number of processing units working on a problem grows, we can solve **bigger problems**.
Parallelism Jargon

- **Threads**: execution sequences that share a single memory area (“address space”)  
- **Processes**: execution sequences with their own independent, private memory areas

… and thus:

- **Multithreading**: parallelism via multiple threads
- **Multiprocessing**: parallelism via multiple processes

As a general rule, Shared Memory Parallelism is concerned with **threads**, and Distributed Parallelism is concerned with **processes**.
Jargon Alert

In principle:
- “shared memory parallelism” ➔ “multithreading”
- “distributed parallelism” ➔ “multiprocessing”

In practice, these terms are often used interchangeably:
- Parallelism
- Concurrency (not as popular these days)
- Multithreading
- Multiprocessing

Typically, you have to figure out what is meant based on the context.
In 1967, Gene Amdahl came up with an idea so crucial to our understanding of parallelism that they named a Law for him:

$$S = \frac{1}{(1 - F_p) + \frac{F_p}{S_p}}$$

where $S$ is the overall speedup achieved by parallelizing a code, $F_p$ is the fraction of the code that’s parallelizable, and $S_p$ is the speedup achieved in the parallel part.[1]
Amdahl’s Law: Huh?

What does Amdahl’s Law tell us?

Imagine that you run your code on a zillion processors. The parallel part of the code could speed up by as much as a factor of a zillion. For sufficiently large values of a zillion, the parallel part would take zero time!

But, the serial (non-parallel) part would take the same amount of time as on a single processor.

So running your code on infinitely many processors would still take at least as much time as it takes to run just the serial part.
Max Speedup by Serial %
Amdahl’s Law Example

```fortran
PROGRAM amdahl_test
  IMPLICIT NONE
  REAL,DIMENSION(a_lot) :: array
  REAL    :: scalar
  INTEGER :: index
  READ *, scalar      !! Serial part
  DO index = 1, a_lot !! Parallel part
    array(index) = scalar * index
  END DO !! index = 1, a_lot
END PROGRAM amdahl_test
```

If we run this program on infinitely many CPUs, then the total run time will still be at least as much as the time it takes to perform the `READ`.
The Point of Amdahl’s Law

**Rule of Thumb**: When you write a parallel code, try to make as much of the code parallel as possible, because the **serial part will be the limiting factor** on parallel speedup.

Note that this rule will not hold when the **overhead** cost of parallelizing exceeds the parallel speedup. More on this presently.
Speedup

The goal in parallelism is **linear speedup**: getting the speed of the job to increase by a factor equal to the number of processors.

Very few programs actually exhibit linear speedup, but some come close.
**Scalability**

*Scalable* means “performs just as well regardless of how big the problem is.” A scalable code has near linear speedup.

![Graph showing ARPS Benchmark Timings](image)

Platinum = NCSA 1024 processor PIII/1GHz Linux Cluster
Note: NCSA Origin timings are scaled from 19x19x53 domains.
Strong vs Weak Scalability

- **Strong Scalability**: If you double the number of processors, but you keep the problem size constant, then the problem takes half as long to complete (i.e., the speed doubles).

- **Weak Scalability**: If you double the number of processors, and double the problem size, then the problem takes the same amount of time to complete (i.e., the speed doubles).
Scalability

This benchmark shows weak scalability.

ARPS Benchmark Timings
19x19x43 3km grid/processor

Platinum = NCSA 1024 processor PIII/1GHZ Linux Cluster
Note: NCSA Origin timings are scaled from 19x19x53 domains.
Granularity

Granularity is the size of the subproblem that each thread or process works on, and in particular the size that it works on between communicating or synchronizing with the others.

Some codes are coarse grain (a few very big parallel parts) and some are fine grain (many little parallel parts).

Usually, coarse grain codes are more scalable than fine grain codes, because less time is spent managing the parallelism, so more is spent getting the work done.
Parallel Overhead

Parallelism isn’t free. Behind the scenes, the compiler and the hardware have to do a lot of overhead work to make parallelism happen.

The overhead typically includes:

- **Managing** the multiple threads/processes
- **Communication** among threads/processes
- **Synchronization** (described later)
Shared Memory Parallelism
The Jigsaw Puzzle Analogy
Serial Computing

Suppose you want to do a jigsaw puzzle that has, say, a thousand pieces.

We can imagine that it’ll take you a certain amount of time. Let’s say that you can put the puzzle together in an hour.
Shared Memory Parallelism

If Horst sits across the table from you, then he can work on his half of the puzzle and you can work on yours. Once in a while, you’ll both reach into the pile of pieces at the same time (you’ll **contend** for the same resource), which will cause a little bit of slowdown. And from time to time you’ll have to work together (**communicate**) at the interface between his half and yours. The speedup will be nearly 2-to-1: y’all might take 35 minutes instead of 30.
The More the Merrier?

Now let’s put Bruce and Dee on the other two sides of the table. Each of you can work on a part of the puzzle, but there’ll be a lot more contention for the shared resource (the pile of puzzle pieces) and a lot more communication at the interfaces. So y’all will get noticeably less than a 4-to-1 speedup, but you’ll still have an improvement, maybe something like 3-to-1: the four of you can get it done in 20 minutes instead of an hour.
Diminishing Returns

If we now put Rebecca and Jen and Alisa and Darlene on the corners of the table, there’s going to be a whole lot of contention for the shared resource, and a lot of communication at the many interfaces. So the speedup y’all get will be much less than we’d like; you’ll be lucky to get 5-to-1.

So we can see that adding more and more workers onto a shared resource is eventually going to have a diminishing return.
Load balancing means giving everyone roughly the same amount of work to do.

For example, if the jigsaw puzzle is half grass and half sky, then you can do the grass and Julie can do the sky, and then y’all only have to communicate at the horizon – and the amount of work that each of you does on your own is roughly equal. So you’ll get pretty good speedup.
Load balancing can be easy, if the problem splits up into chunks of roughly equal size, with one chunk per processor. Or load balancing can be very hard.
How Shared Memory Parallelism Behaves
The Fork/Join Model

Many shared memory parallel systems use a programming model called **Fork/Join**. Each program begins executing on just a single thread, called the **parent**.

**Fork**: When a parallel region is reached, the parent thread *spawns* additional **child** threads as needed.

**Join**: When the parallel region ends, the child threads shut down, leaving only the parent still running.
The Fork/Join Model (cont’d)

Parent Thread
Start

Fork

Overhead

Child Threads

Join

End

Overhead

Compute time
The Fork/Join Model (cont’d)

In principle, as a parallel section completes, the child threads shut down (join the parent), forking off again when the parent reaches another parallel section.

In practice, the child threads often continue to exist but are **idle**.

Why?
Principle vs. Practice
Why Idle?

On some shared memory multithreading computers, the **overhead cost** of forking and joining is **high** compared to the cost of computing, so rather than waste time on overhead, the **children sit idle** until the next parallel section.

On some computers, joining threads releases a program’s control over the child processors, so they may not be available for more parallel work later in the run. **Gang scheduling** is preferable, because then all of the processors are guaranteed to be available for the whole run.
OpenMP

Most of this discussion is from [2], with a little bit from [3].
What Is OpenMP?

OpenMP is a standardized way of expressing shared memory parallelism.

OpenMP consists of **compiler directives**, **functions** and **environment variables**.

When you compile a program that has OpenMP in it, if your compiler knows OpenMP, then you get an executable that can run in parallel; otherwise, the compiler ignores the OpenMP stuff and you get a purely serial executable.

OpenMP can be used in Fortran, C and C++, but only if your preferred compiler explicitly supports it.
Compiler Directives

A *compiler directive* is a line of source code that gives the compiler special information about the statement or block of code that immediately follows.

C++ and C programmers already know about compiler directives:

```
#include "MyClass.h"
```

Many Fortran programmers already have seen at least one compiler directive:

```
INCLUDE 'mycommon.inc'
```
OpenMP Compiler Directives

OpenMP compiler directives in Fortran look like this:

```fortran
! $OMP ...stuff...
```

In C++ and C, OpenMP directives look like:

```c
#pragma omp ...stuff...
```

Both directive forms mean “the rest of this line contains OpenMP information.”

Aside: “pragma” is the Greek word for “thing.” Go figure.
### Example OpenMP Directives

<table>
<thead>
<tr>
<th>Fortran</th>
<th>C++/C</th>
</tr>
</thead>
<tbody>
<tr>
<td>!$OMP PARALLEL DO</td>
<td>#pragma omp parallel for</td>
</tr>
<tr>
<td>!$OMP CRITICAL</td>
<td>#pragma omp critical</td>
</tr>
<tr>
<td>!$OMP MASTER</td>
<td>#pragma omp master</td>
</tr>
<tr>
<td>!$OMP BARRIER</td>
<td>#pragma omp barrier</td>
</tr>
<tr>
<td>!$OMP SINGLE</td>
<td>#pragma omp single</td>
</tr>
<tr>
<td>!$OMP ATOMIC</td>
<td>#pragma omp atomic</td>
</tr>
<tr>
<td>!$OMP SECTION</td>
<td>#pragma omp section</td>
</tr>
<tr>
<td>!$OMP FLUSH</td>
<td>#pragma omp flush</td>
</tr>
<tr>
<td>!$OMP ORDERED</td>
<td>#pragma omp ordered</td>
</tr>
</tbody>
</table>

Note that we won’t cover all of these.
A First OpenMP Program

PROGRAM hello_world
IMPLICIT NONE
INTEGER :: number_of_threads, this_thread, iteration
INTEGER,EXTERNAL :: omp_get_max_threads, omp_get_thread_num

number_of_threads = omp_get_max_threads()
WRITE (0,"(I2,A)") number_of_threads, " threads"
!$OMP PARALLEL DO DEFAULT(PRIVATE) &
!$OMP SHARED(number_of_threads)
DO iteration = 0, number_of_threads - 1
   this_thread = omp_get_thread_num()
   WRITE (0,"(A,I2,A,I2,A) ")"Iteration ", &
   & iteration, ", thread ", this_thread, &
   & ": Hello, world!"
END DO
END PROGRAM hello_world
Running \texttt{hello\_world}

\begin{verbatim}
% setenv OMP_NUM_THREADS 4
% hello_world
  4 threads
 Iteration 0, thread 0: Hello, world!
 Iteration 1, thread 1: Hello, world!
 Iteration 3, thread 3: Hello, world!
 Iteration 2, thread 2: Hello, world!
% hello_world
  4 threads
 Iteration 2, thread 2: Hello, world!
 Iteration 1, thread 1: Hello, world!
 Iteration 0, thread 0: Hello, world!
 Iteration 3, thread 3: Hello, world!
% hello_world
  4 threads
 Iteration 1, thread 1: Hello, world!
 Iteration 2, thread 2: Hello, world!
 Iteration 0, thread 0: Hello, world!
 Iteration 3, thread 3: Hello, world!
\end{verbatim}
OpenMP Issues Observed

From the `hello_world` program, we learn that:

- At some point before running an OpenMP program, you must set an environment variable `OMP_NUM_THREADS` that represents the number of threads to use.
- The order in which the threads execute is **nondeterministic**.
The PARALLEL DO Directive

The PARALLEL DO directive tells the compiler that the DO loop immediately after the directive should be executed in parallel; for example:

```c
!$OMP PARALLEL DO
  DO index = 1, length
    array(index) = index * index
  END DO
```

The iterations of the loop will be computed in parallel (note that they are independent of one another).
A Change to `hello_world`

Suppose we do 3 loop iterations per thread:

```fortran
DO iteration = 0, number_of_threads * 3 - 1
  
% hello_world
  4 threads
Iteration 9, thread 3: Hello, world!
Iteration 0, thread 0: Hello, world!
Iteration 10, thread 3: Hello, world!
Iteration 11, thread 3: Hello, world!
Iteration 1, thread 0: Hello, world!
Iteration 2, thread 0: Hello, world!
Iteration 3, thread 1: Hello, world!
Iteration 6, thread 2: Hello, world!
Iteration 7, thread 2: Hello, world!
Iteration 8, thread 2: Hello, world!
Iteration 4, thread 1: Hello, world!
Iteration 5, thread 1: Hello, world!
```

Notice that the iterations are split into contiguous **chunks**, and each thread gets one chunk of iterations.
Chunks

By default, OpenMP splits the iterations of a loop into chunks of equal (or roughly equal) size, assigns each chunk to a thread, and lets each thread loop through its subset of the iterations.

So, for example, if you have 4 threads and 12 iterations, then each thread gets three iterations:

- Thread 0: iterations 0, 1, 2
- Thread 1: iterations 3, 4, 5
- Thread 2: iterations 6, 7, 8
- Thread 3: iterations 9, 10, 11

Notice that each thread performs its own chunk in deterministic order, but that the overall order is nondeterministic.
Private and Shared Data

**Private** data are data that are owned by, and only visible to, a single individual thread.

**Shared** data are data that are owned by and visible to all threads.

(Note: In distributed parallelism, all data are private, as we’ll see next time.)
Should All Data Be Shared?

In our example program, we saw this:

```
!$OMP PARALLEL DO DEFAULT(PRIVATE) SHARED(number_of_threads)
```

What do `DEFAULT(PRIVATE)` and `SHARED` mean?

We said that OpenMP uses shared memory parallelism. So `PRIVATE` and `SHARED` refer to memory.

Would it make sense for all data within a parallel loop to be shared?
A Private Variable

Consider this loop:

```c
!$OMP PARALLEL DO ...
  DO iteration = 0, number_of_threads - 1
    this_thread = omp_get_thread_num()
    WRITE (0,"(A,I2,A,I2,A) "") "Iteration ", iteration, 
    &
    "", thread ", this_thread, ": Hello, world!"
  END DO
```

Notice that, if the iterations of the loop are executed concurrently, then the loop index variable named `iteration` will be wrong for all but one of the threads.

Each thread should get its own copy of the variable named `iteration`. 
Another Private Variable

!$OMP PARALLEL DO ...
   DO iteration = 0, number_of_threads - 1
       this_thread = omp_get_thread_num()
       WRITE (0,"(A,I2,A,I2,A)") "Iteration ", iteration, 
           &, 
           "thread ", this_thread, ": Hello, world!"
   END DO

Notice that, if the iterations of the loop are executed concurrently, then this_thread will be wrong for all but one of the threads.

Each thread should get its own copy of the variable named this_thread.
A Shared Variable

```fortran
!$OMP PARALLEL DO 
  DO iteration = 0, number_of_threads - 1 
    this_thread = omp_get_thread_num() 
    WRITE (0,"(A,I2,A,I2,A)""") "Iteration ", iteration, & 
    ", thread ", this_thread, ": Hello, world!" 
  END DO 

Notice that, regardless of whether the iterations of the loop are 
executed serially or in parallel, **number_of_threads** 
will be correct for all of the threads. 

All threads should share a single instance of **number_of_threads**.
```
SHARED & PRIVATE Clauses

The **PARALLEL DO** directive allows extra *clauses* to be appended that tell the compiler which variables are shared and which are private:

```
!$OMP PARALLEL DO PRIVATE(iteration,this_thread) &
!$OMP SHARED (number_of_threads)
```

This tells that compiler that *iteration* and *this_thread* are private but that *number_of_threads* is shared.

(Note the syntax for continuing a directive in Fortran90.)
DEFAULT Clause

If your loop has lots of variables, it may be cumbersome to put all of them into \texttt{SHARED} and \texttt{PRIVATE} clauses.

So, OpenMP allows you to declare one kind of data to be the default, and then you only need to explicitly declare variables of the other kind:

\begin{verbatim}
!$OMP PARALLEL DO DEFAULT(PRIVATE) &
!$OMP             SHARED(number_of_threads)
\end{verbatim}

The default \texttt{DEFAULT} (so to speak) is \texttt{SHARED}, except for the loop index variable, which by default is \texttt{PRIVATE}.
Different Workloads

What happens if the threads have different amounts of work to do?

```!
!$OMP PARALLEL DO
DO index = 1, length
  x(index) = index / 3.0
  IF (x(index) < 0) THEN
    y(index) = LOG(x(index))
  ELSE
    y(index) = 1.0 - x(index)
  END IF
END DO
```

The threads that finish early have to wait.
Chunks

By default, OpenMP splits the iterations of a loop into chunks of equal (or roughly equal) size, assigns each chunk to a thread, and lets each thread loop through its subset of the iterations.

So, for example, if you have 4 threads and 12 iterations, then each thread gets three iterations:

- Thread 0: iterations 0, 1, 2
- Thread 1: iterations 3, 4, 5
- Thread 2: iterations 6, 7, 8
- Thread 3: iterations 9, 10, 11

Notice that each thread performs its own chunk in deterministic order, but that the overall order is nondeterministic.
Scheduling Strategies

OpenMP supports three scheduling strategies:

- **Static**: The default, as described in the previous slides – good for iterations that are inherently load balanced.

- **Dynamic**: Each thread gets a chunk of a few iterations, and when it finishes that chunk it goes back for more, and so on until all of the iterations are done – good when iterations aren’t load balanced at all.

- **Guided**: Each thread gets smaller and smaller chunks over time – a compromise.
Static Scheduling

For $N_i$ iterations and $N_t$ threads, each thread gets one chunk of $N_i/N_t$ loop iterations:

For $N_i$ iterations and $N_t$ threads, each thread gets one chunk of $N_i/N_t$ loop iterations:

- Thread #0: iterations 0 through $N_i/N_t-1$
- Thread #1: iterations $N_i/N_t$ through $2N_i/N_t-1$
- Thread #2: iterations $2N_i/N_t$ through $3N_i/N_t-1$
- ...  
- Thread #$N_t-1$: iterations $(N_t-1)N_i/N_t$ through $N_i-1$
Dynamic Scheduling

For $N_i$ iterations and $N_t$ threads, each thread gets a fixed-size chunk of $k$ loop iterations:

```
T0  T1  T2  T3  T4  T5  T2  T3  T4  T0  T1  T5  T3  T2
```

When a particular thread finishes its chunk of iterations, it gets assigned a new chunk. So, the relationship between iterations and threads is nondeterministic.

- Advantage: very flexible
- Disadvantage: high overhead – lots of decision making about which thread gets each chunk
Guided Scheduling

For \( N_i \) iterations and \( N_t \) threads, initially each thread gets a fixed-size chunk of \( k < N_i / N_t \) loop iterations:

\[
\begin{array}{cccccccccccc}
T0 & T1 & T2 & T3 & T4 & T5 & 2 & 3 & 4 & 1 & 0 & 2 & 5 & 4 & 2 & 3 & 1 \\
\end{array}
\]

After each thread finishes its chunk of \( k \) iterations, it gets a chunk of \( k/2 \) iterations, then \( k/4 \), etc. Chunks are assigned dynamically, as threads finish their previous chunks.

- Advantage over static: can handle imbalanced load
- Advantage over dynamic: fewer decisions, so less overhead
How to Know Which Schedule?

Test all three using a typical case as a benchmark. Whichever wins is probably the one you want to use most of the time on that particular platform.

This may vary depending on problem size, new versions of the compiler, who’s on the machine, what day of the week it is, etc, so you may want to benchmark the three schedules from time to time.
The `PARALLEL DO` directive allows a `SCHEDULE` clause to be appended that tell the compiler which variables are shared and which are private:

\[
!$OMP PARALLEL DO ... SCHEDULE (STATIC)
\]

This tells that compiler that the schedule will be static.
Likewise, the schedule could be `GUIDED` or `DYNAMIC`.
However, the very best schedule to put in the `SCHEDULE` clause is `RUNTIME`.
You can then set the environment variable `OMP_SCHEDULE` to `STATIC` or `GUIDED` or `DYNAMIC` at runtime – great for benchmarking!
**Synchronization**

**Jargon**: Waiting for other threads to finish a parallel loop (or other parallel section) before going on to the work after the parallel section is called *synchronization*.

Synchronization is **BAD**, because when a thread is waiting for the others to finish, it isn’t getting any work done, so it isn’t contributing to speedup.

So why would anyone ever synchronize?
Why Synchronize?

Synchronizing is necessary when the code that follows a parallel section needs all threads to have their final answers.

```plaintext
!$OMP PARALLEL DO
  DO index = 1, length
    x(index) = index / 1024.0
    IF ((index / 1000) < 1) THEN
      y(index) = LOG(x(index))
    ELSE
      y(index) = x(index) + 2
    END IF
  END DO
! Need to synchronize here!
  DO index = 1, length
    z(index) = y(index) + y(length - index + 1)
  END DO
```
Barriers

A **barrier** is a place where synchronization is forced to occur; that is, where faster threads have to wait for slower ones.

The **PARALLEL DO** directive automatically puts an invisible, implied barrier at the end of its **DO** loop:

```
!$OMP PARALLEL DO
  DO index = 1, length
    ... parallel stuff ...
  END DO
! Implied barrier
  ... serial stuff ...
```

OpenMP also has an explicit **BARRIER** directive, but most people don’t need it.
Critical Sections

A **critical section** is a piece of code that any thread can execute, but that only one thread can execute at a time.

```Fortran
!$OMP PARALLEL DO
  DO index = 1, length
    ... parallel stuff ...
  !$OMP CRITICAL(summing)
    sum = sum + x(index) * y(index)
  !$OMP END CRITICAL(summing)
    ... more parallel stuff ...
  END DO
```

What’s the point?
Why Have Critical Sections?

If only one thread at a time can execute a critical section, that slows the code down, because the other threads may be waiting to enter the critical section.

But, for certain statements, if you don’t ensure *mutual exclusion*, then you can get nondeterministic results.
If No Critical Section

```cpp
!$OMP CRITICAL(summing)
    sum = sum + x(index) * y(index)
!$OMP END CRITICAL(summing)
```

Suppose for thread #0, `index` is 27, and for thread #1, `index` is 92.

If the two threads execute the above statement at the same time, `sum` could be
- the value after adding `x(27) * y(27)`, or
- the value after adding `x(92) * y(92)`, or
- garbage!

This is called a `race condition`: the result depends on who wins the race.
Pen Game #1: Take the Pen

We need two volunteers for this game.
1. I’ll hold a pen in my hand.
2. You win by taking the pen from my hand.
3. One, two, three, go!

Can we predict the outcome? Therefore, can we guarantee that we get the correct outcome?
Pen Game #2: Look at the Pen

We need two volunteers for this game.

1. I’ll hold a pen in my hand.
2. You win by looking at the pen.
3. One, two, three, go!

Can we predict the outcome? Therefore, can we guarantee that we get the correct outcome?
Race Conditions

A *race condition* is a situation in which multiple processes can change the value of a variable at the same time.

As in Pen Game #1 (Take the Pen), a race condition can lead to unpredictable results.

So, race conditions are **BAD**.
Reductions

A reduction converts an array to a scalar: sum, product, minimum value, maximum value, location of minimum value, location of maximum value, Boolean AND, Boolean OR, number of occurrences, etc.

Reductions are so common, and so important, that OpenMP has a specific construct to handle them: the **REDUCTION** clause in a **PARALLEL DO** directive.
Reduction Clause

```c
total_mass = 0
!$OMP PARALLEL DO REDUCTION(+:total_mass)
    DO index = 1, length
        total_mass = total_mass + mass(index)
    END DO !! index = 1, length

This is equivalent to:

```c
total_mass = 0
DO thread = 0, number_of_threads - 1
    thread_mass(thread) = 0
END DO
$OMP PARALLEL DO
    DO index = 1, length
        thread = omp_get_thread_num()
        thread_mass(thread) = thread_mass(thread) + mass(index)
    END DO !! index = 1, length
    DO thread = 0, number_of_threads - 1
        total_mass = total_mass + thread_mass(thread)
    END DO```

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Parallelizing a Serial Code #1

```fortran
PROGRAM big_science
    ... declarations ...
    DO ...
        ... parallelizable work ...
    END DO
    ... serial work ...
    DO ...
        ... more parallelizable work ...
    END DO
    ... serial work ...
    ... etc ...
    END PROGRAM big_science
```

```fortran
PROGRAM big_science
    ... declarations ...
    !$OMP PARALLEL DO ...
    DO ...
        ... parallelizable work ...
    END DO
    ... serial work ...
    !$OMP PARALLEL DO ...
    DO ...
        ... more parallelizable work ...
    END DO
    ... serial work ...
    ... etc ...
    END PROGRAM big_science
```

This way may have lots of **synchronization** overhead.
Parallelizing a Serial Code #2

PROGRAM big_science
    ... declarations ...

    DO task = 1, numtasks
        CALL science_task(…)
    END DO
END PROGRAM big_science

SUBROUTINE science_task (…)
    ... parallelizable work ...

    ... serial work ...

    ... more parallelizable work ...

    ... serial work ...

    ... etc ...
END PROGRAM big_science

PROGRAM big_science
    ... declarations ...

    !$OMP PARALLEL DO ...
        DO task = 1, numtasks
            CALL science_task(…)
        END DO
    END !$OMP PARALLEL DO ...
END PROGRAM big_science

SUBROUTINE science_task (…)
    ... parallelizable work ...

    !$OMP MASTER ...
        ... serial work ...
    !$OMP END MASTER ...

    ... more parallelizable work ...

    !$OMP MASTER ...
        ... serial work ...
    !$OMP END MASTER ...

    ... etc ...
END PROGRAM big_science
To Learn More Supercomputing

http://www.oscer.ou.edu/education.php
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Questions?
References